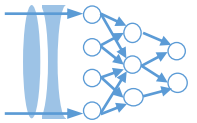


Lecture 16: Introduction to Physical Layers in Machine Learning

Machine Learning and Imaging

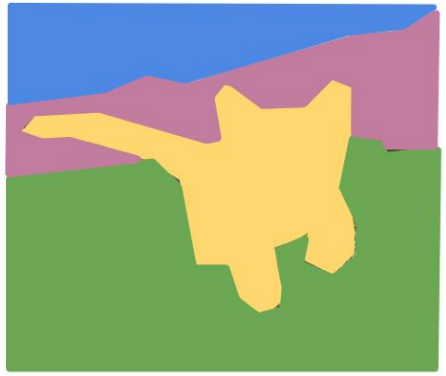
BME 548L
Roarke Horstmeyer

Notes

- Homework 3 released soon!
- I'll review final project proposals this week and will provide feedback

Other Computer Vision Tasks

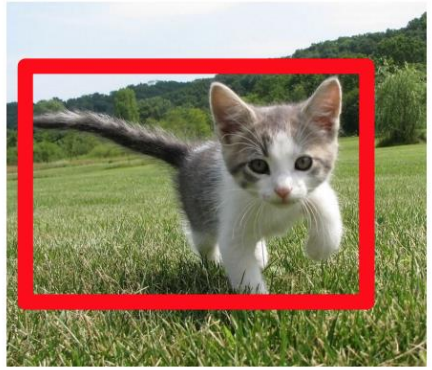
Semantic Segmentation



GRASS, CAT, TREE, SKY

No objects, just pixels

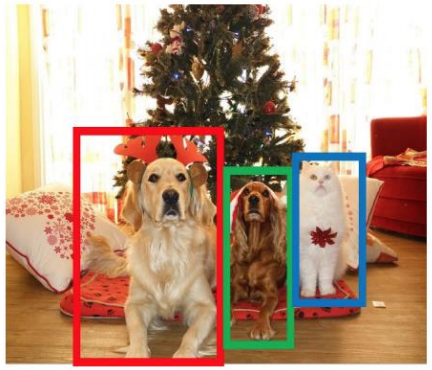
Classification + Localization



CAT

Single Object

Object Detection



DOG, DOG, CAT

Instance Segmentation

DOG, DOG, CAT

Multiple Object

Super-resolution

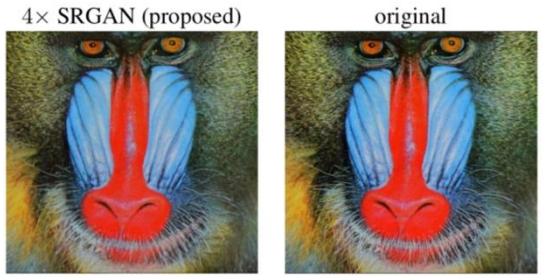


Figure 1: Super-resolved image (left) is almost indistinguishable from original (right). [4× upscaling]

Balanced equation

Over-determined

Over-determined

Over-determined

Under-determined

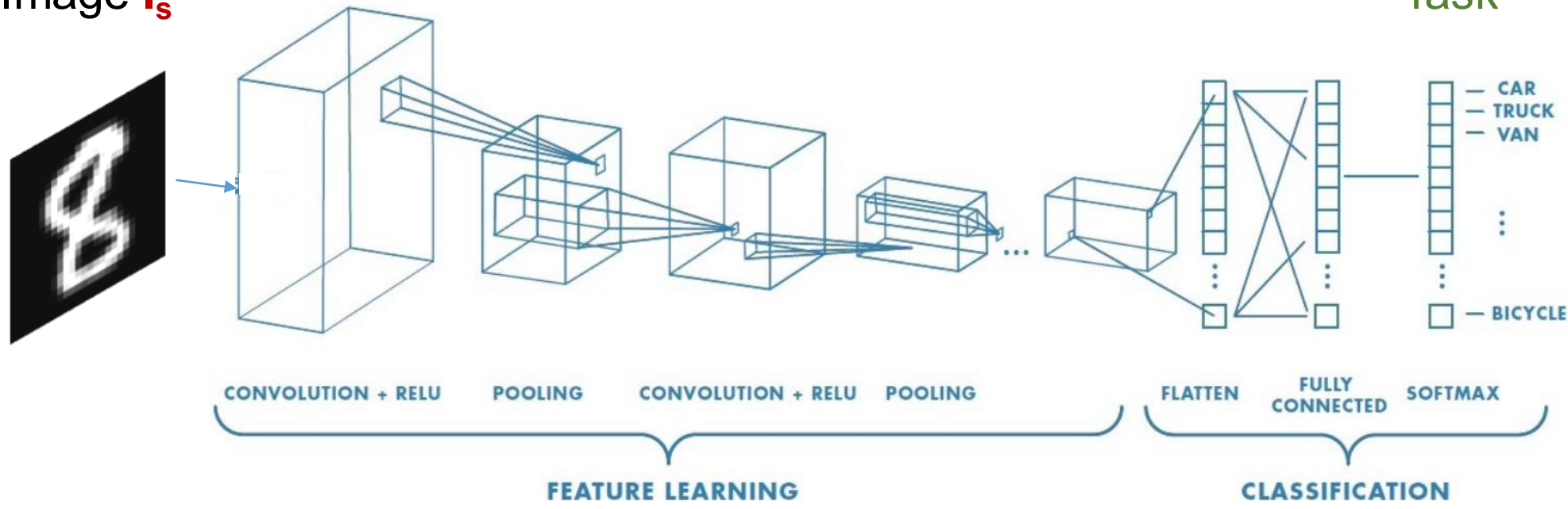
Stanford CS231n - http://cs231n.stanford.edu

Bringing together physical and digital image representations

deep imaging

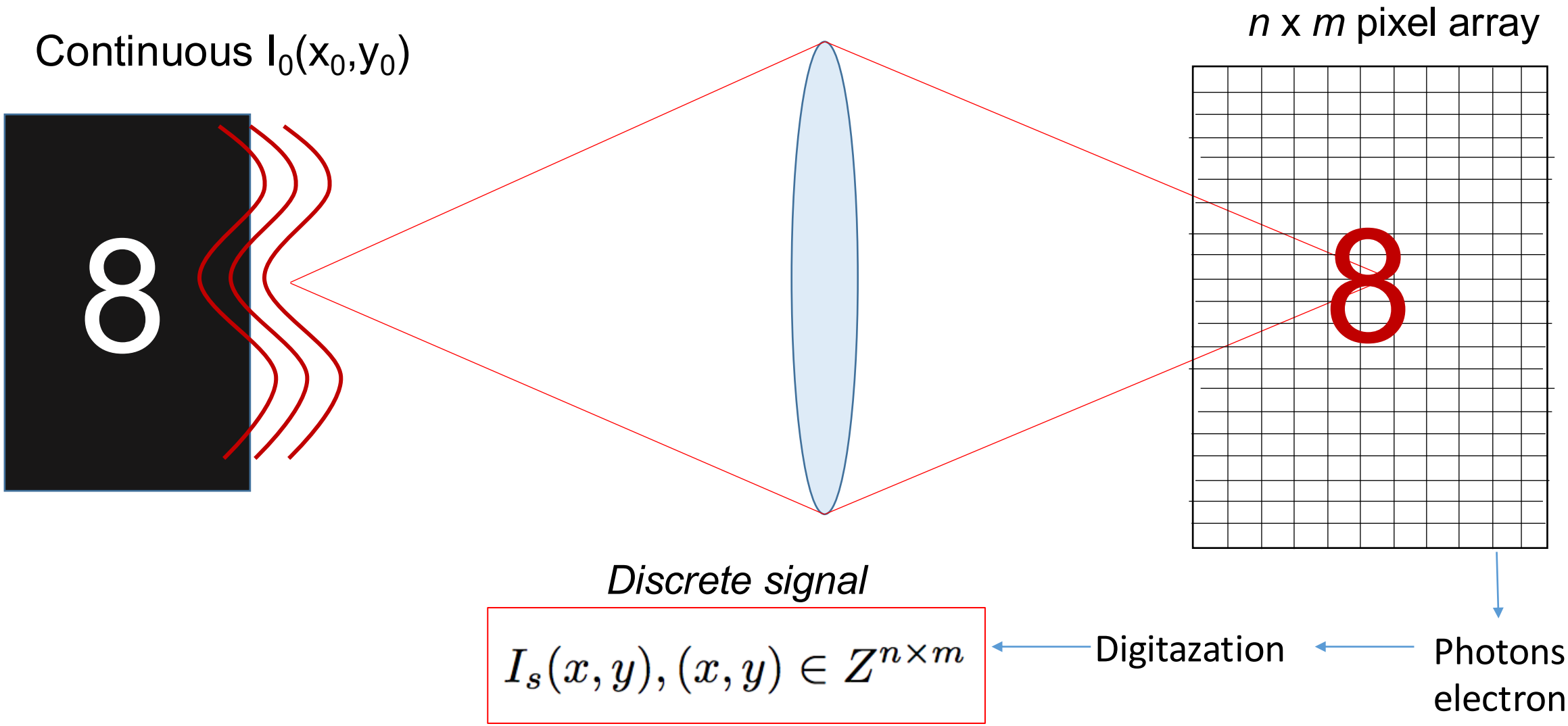
Image I_s

Task

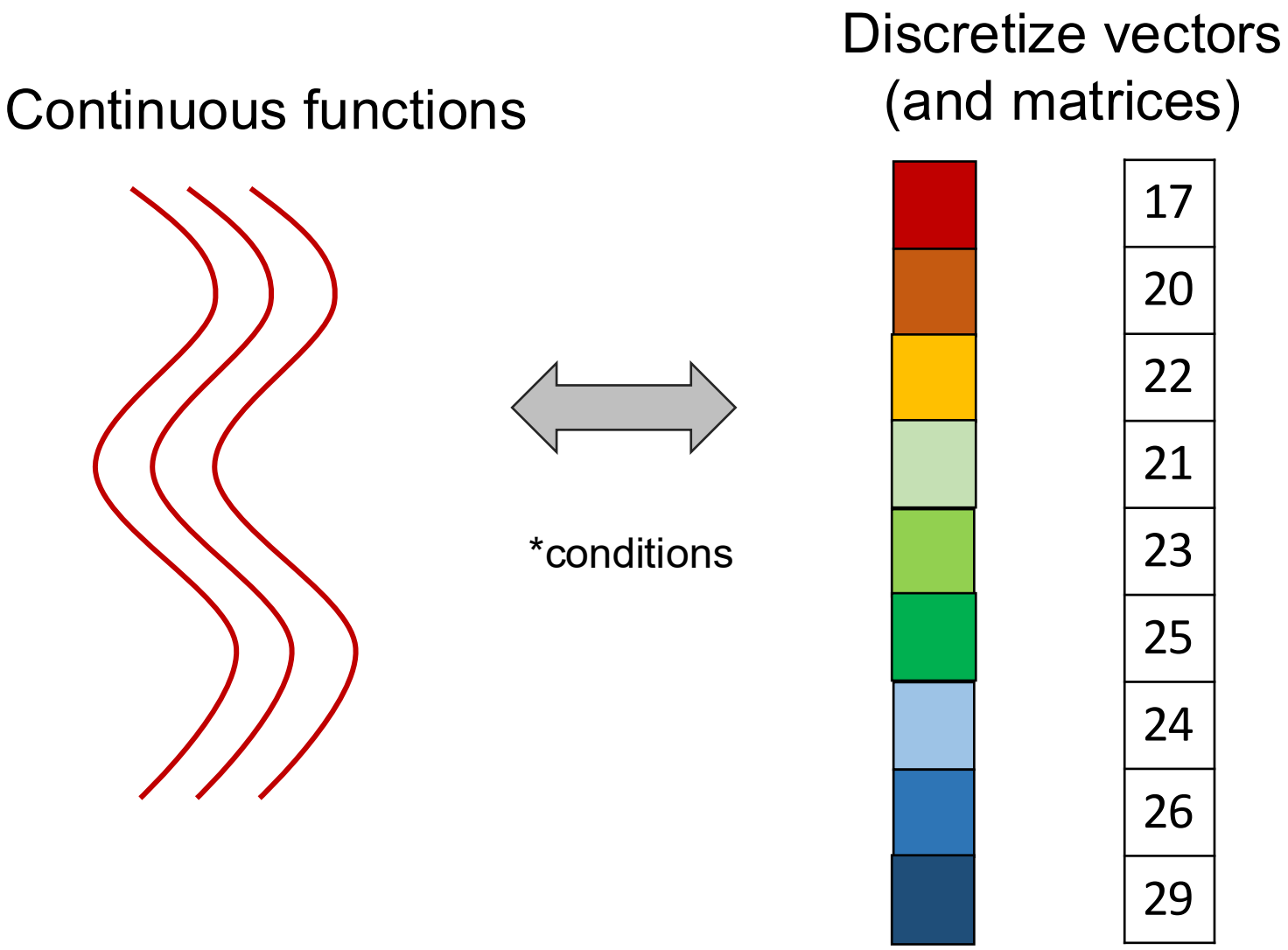


Task = $\mathbf{W_n}$ …ReLU[$\mathbf{W_1}$ ReLU[$\mathbf{W_0}$ I_s]…]

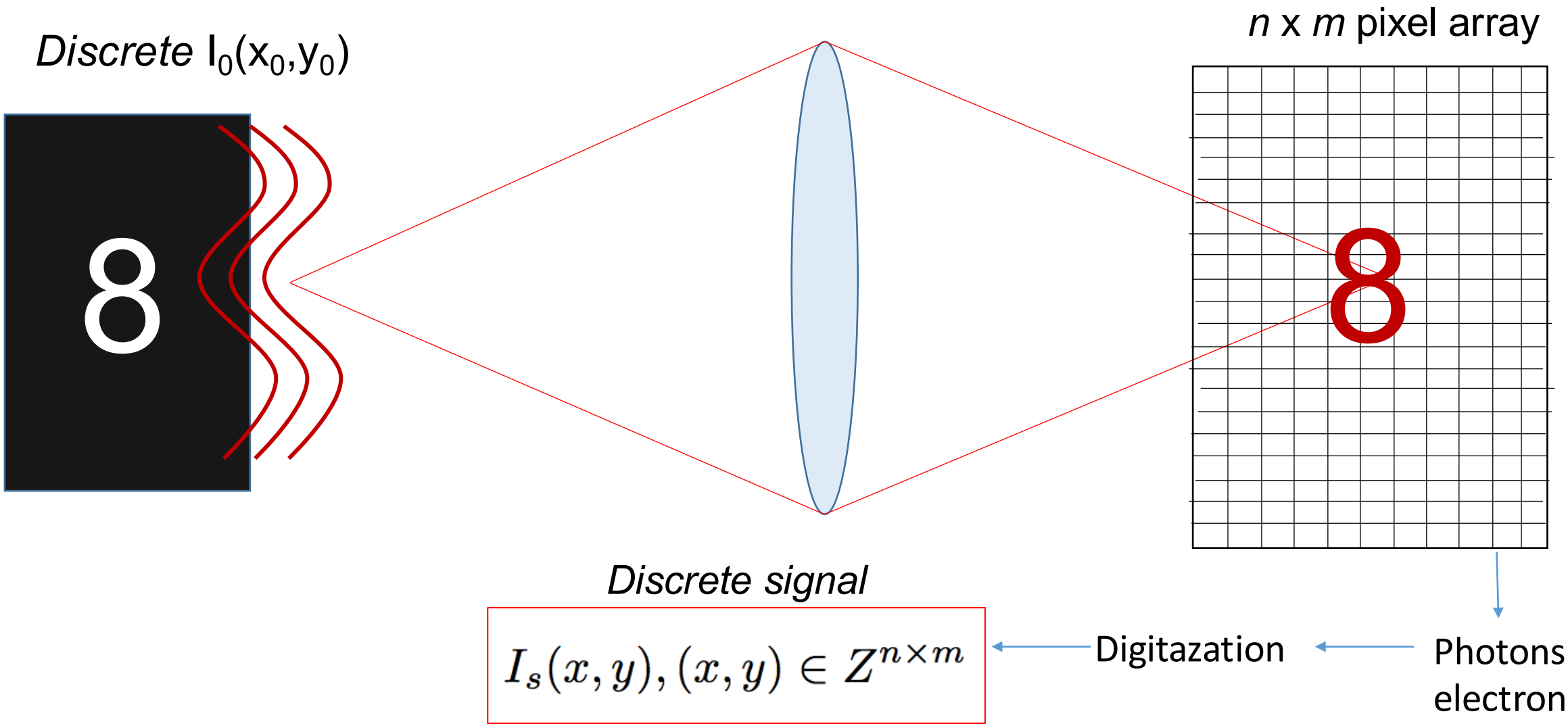
Simple model of image formation



What does the Sampling Theorem mean for us?



Simple model of image formation



Bringing together physical and digital image representations

deep imaging

Physical Layers

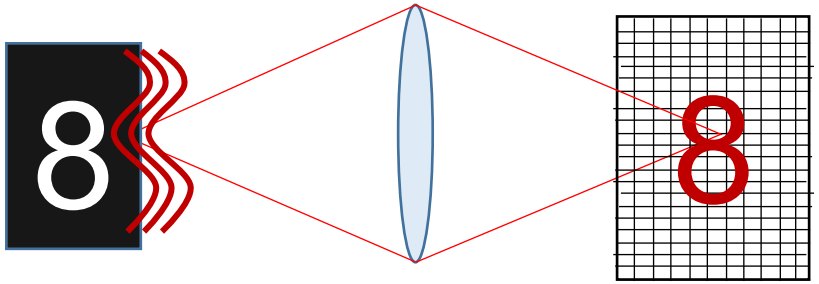
Digital Layers

Physical world

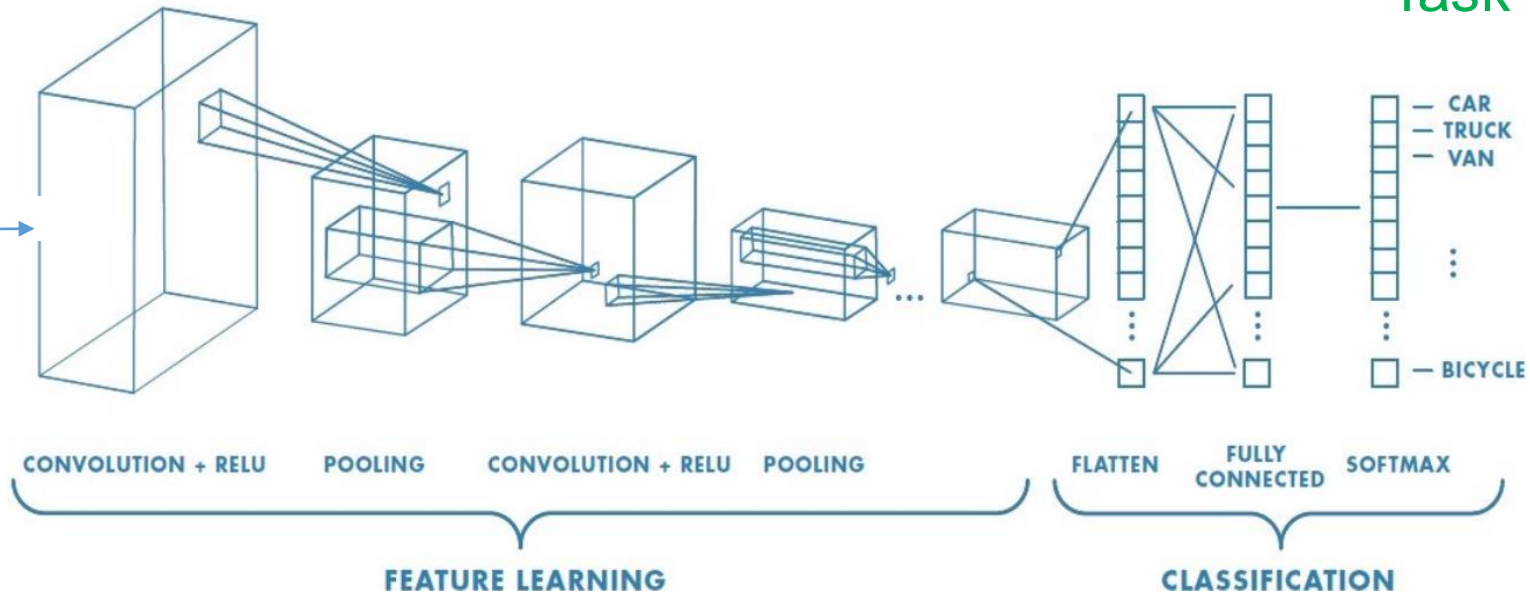
$I_0(x_0,y_0)$

Digital Image

$I_s(x,y)$



Task



$$I_s = f[I_0]$$

Digital layers

Physical layers

$$\text{Task} = W_n \ldots \text{ReLU}[W_1 \, \text{ReLU}[W_0 \, f[I_0]]\ldots]$$

Bringing together physical and digital image representations

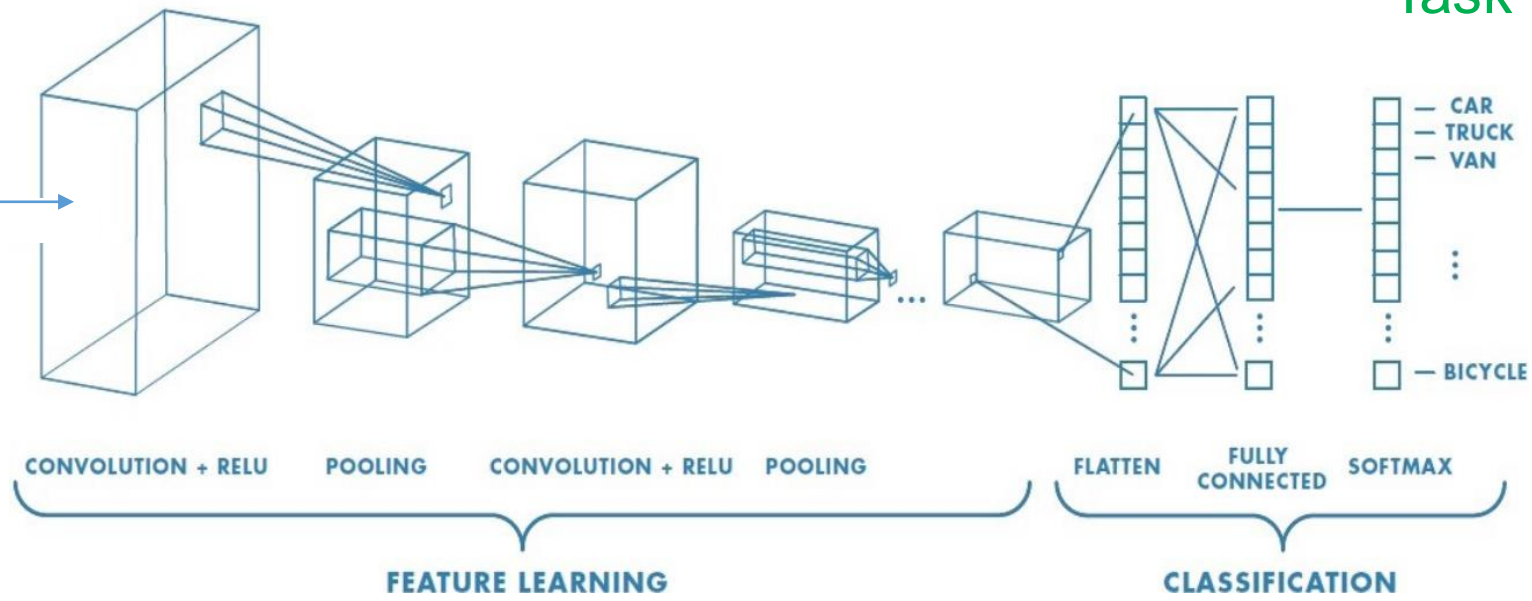
deep imaging

Physical Layers

Digital Layers

Task

Physical Function I_0 → f[ ] → Digitized I_s →



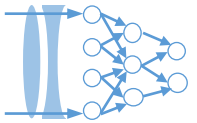
$$I_s = f[I_0]$$

Digital layers

Physical layers

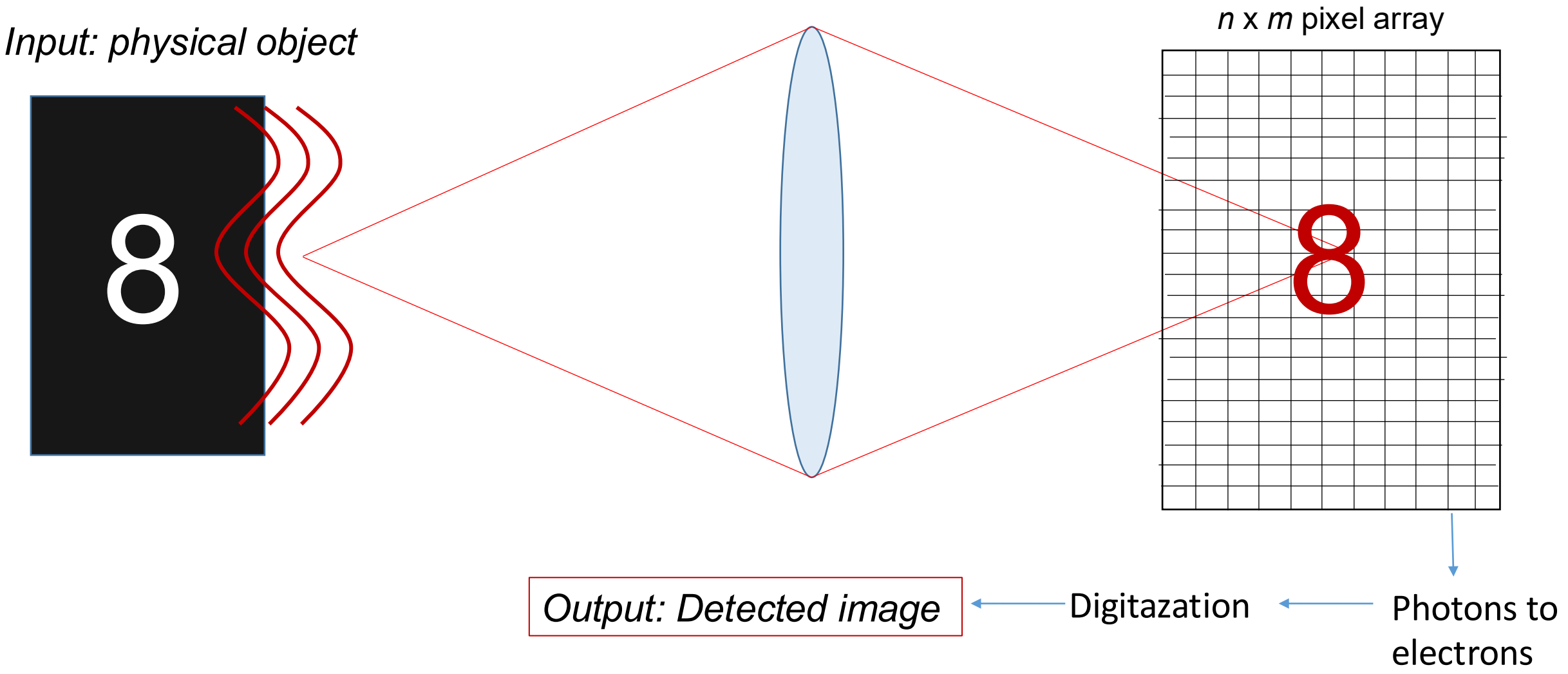
$$\text{Task} = W_n \ldots \text{ReLU}[W_1 \, \text{ReLU}[W_0 \, f[I_0]]\ldots]$$

Required properties of physical mapping f[ ] for DNN optimization?



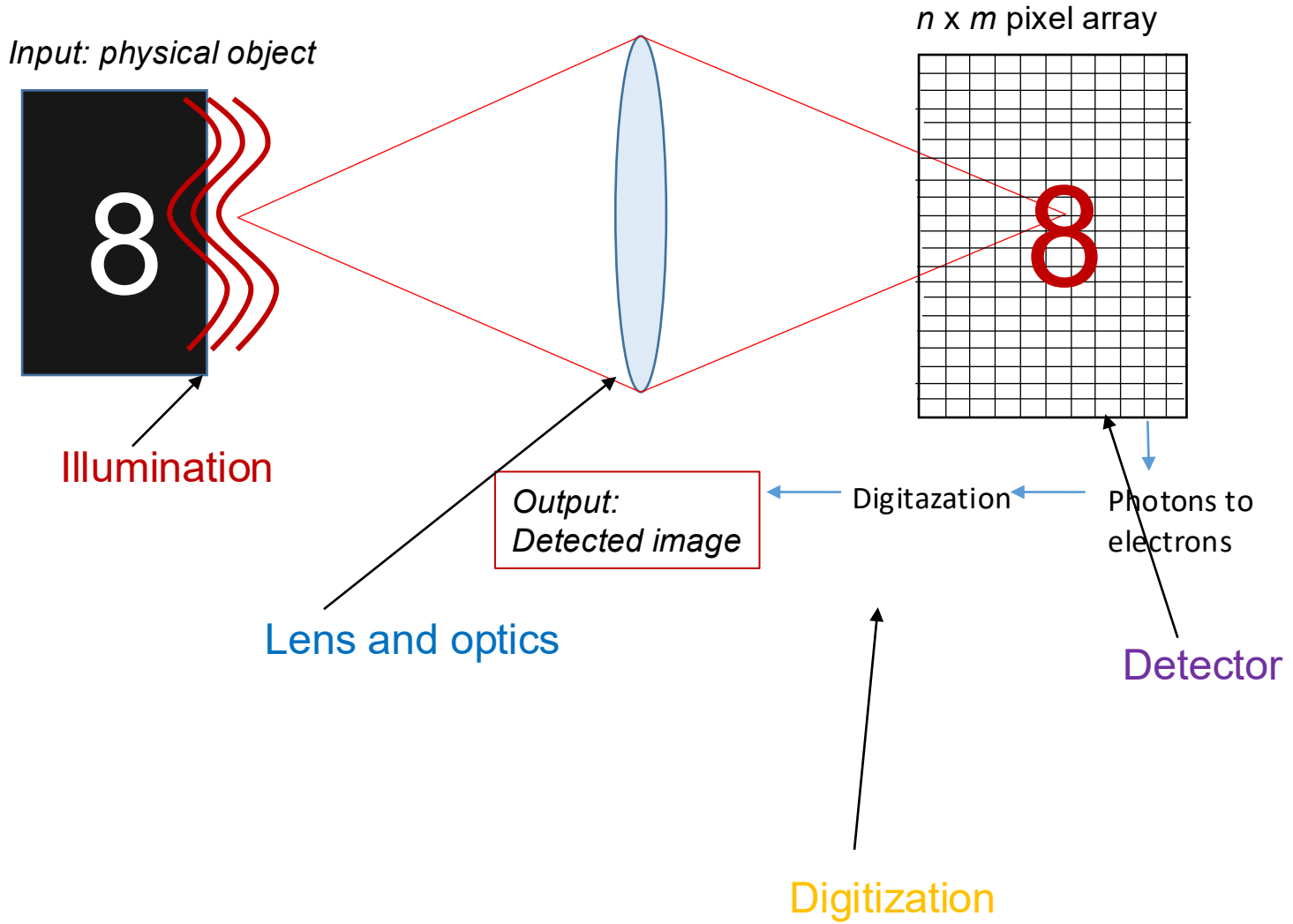
- Finite
- Non-zero gradients
- Differentiable*
- Known structure (for now…)
- Anything else?

What physical parameters effect image formation?

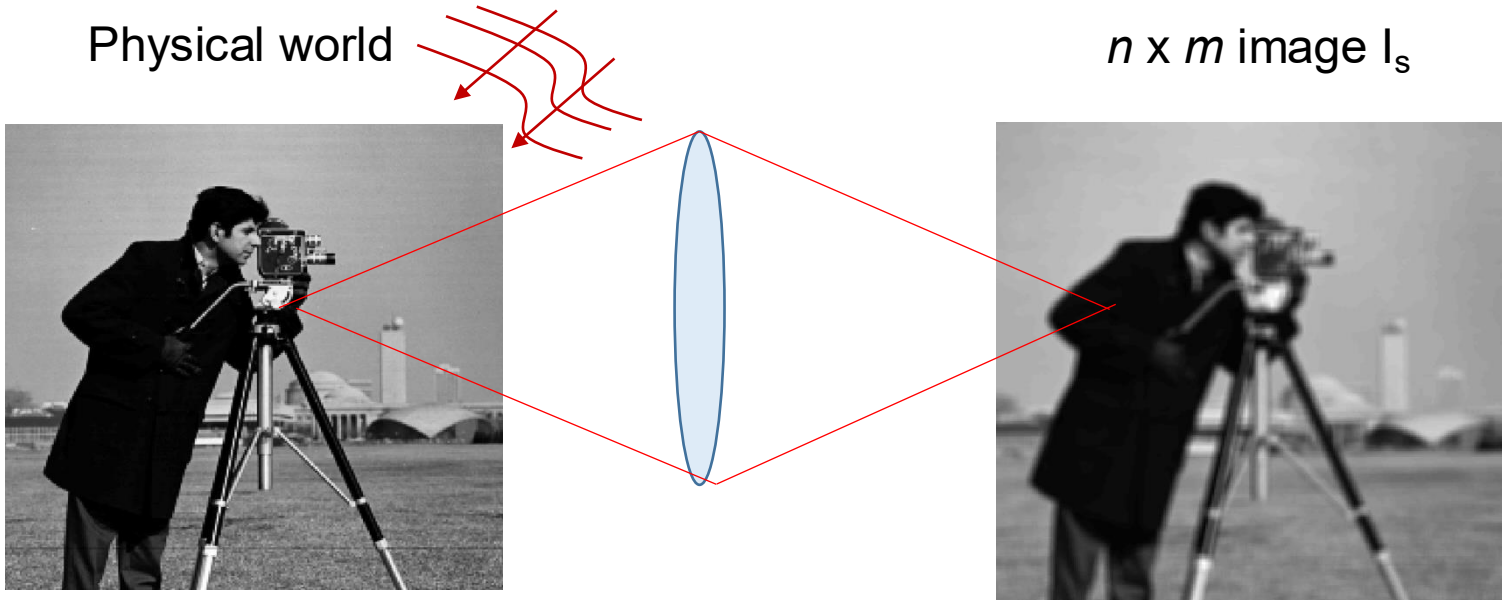


What physical parameters effect image formation?

- Illumination
  - Spatial pattern
  - Angle of incidence
  - Color, polarization
- Lens and optics
  - Position/orientation
  - Shape
  - Focus
  - Transparency
- Detector
  - Pixel size
  - Pixel shape & fill factor
  - Color filters
  - Other filters
- Digitization
  - E to P curves
  - Digitization schemes/thresholds
  - Data transmission, multiplexing
- Physical object

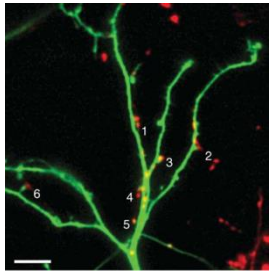


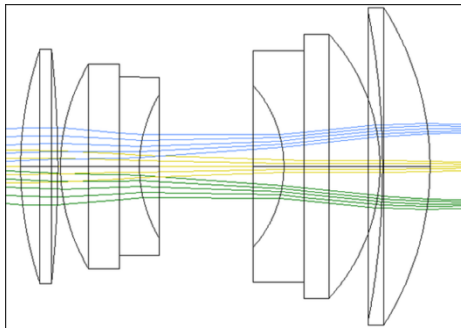
Simple mathematical model of image formation



First - what is light and how can we model it?

- Interpretation #1: Radiation (*Incoherent*)
- Model: Rays



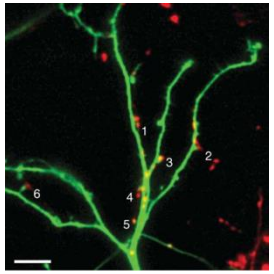


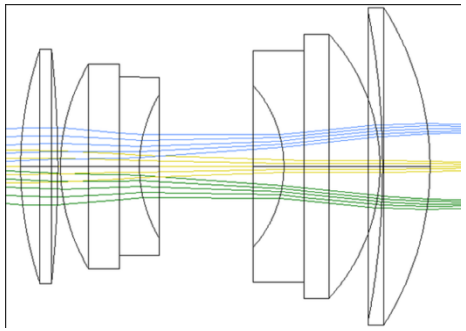
- Real, non-negative
- Models absorption and brightness

$$I_{tot} = I_1 + I_2$$

First - what is light and how can we model it?

- Interpretation #1: Radiation (*Incoherent*)
- Model: Rays

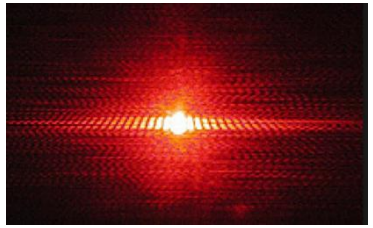


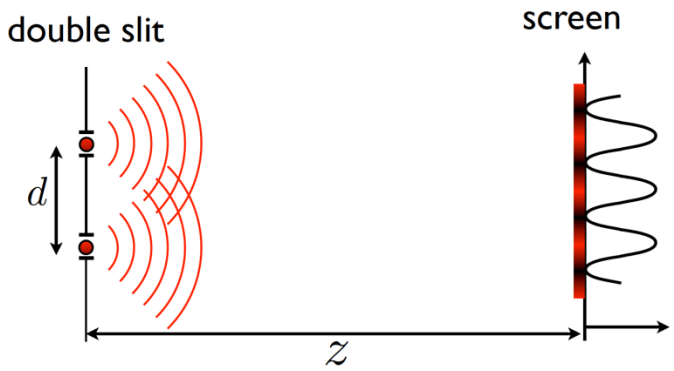


- Real, non-negative
- Models absorption and brightness

$$I_{tot} = I_1 + I_2$$

- Interpretation #2: Electromagnetic wave (*Coherent*)
- Model: Waves



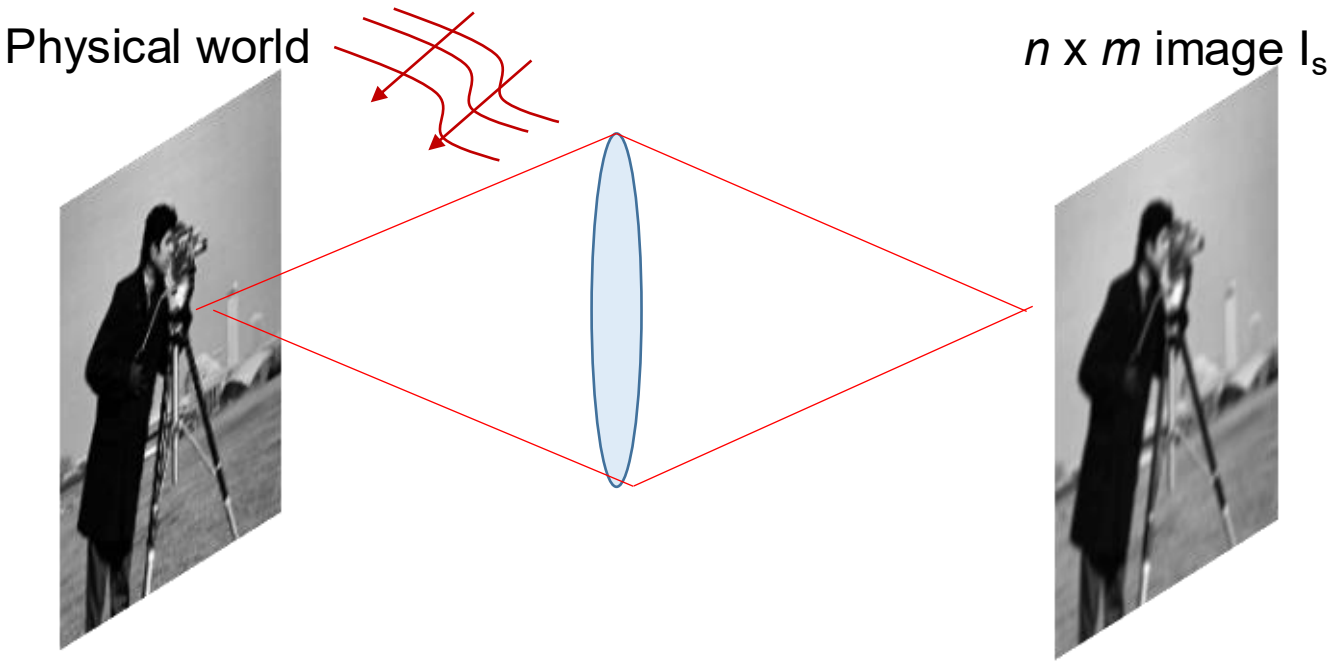


- Complex field
- Models Interference

$$E_{tot} = E_1 + E_2$$

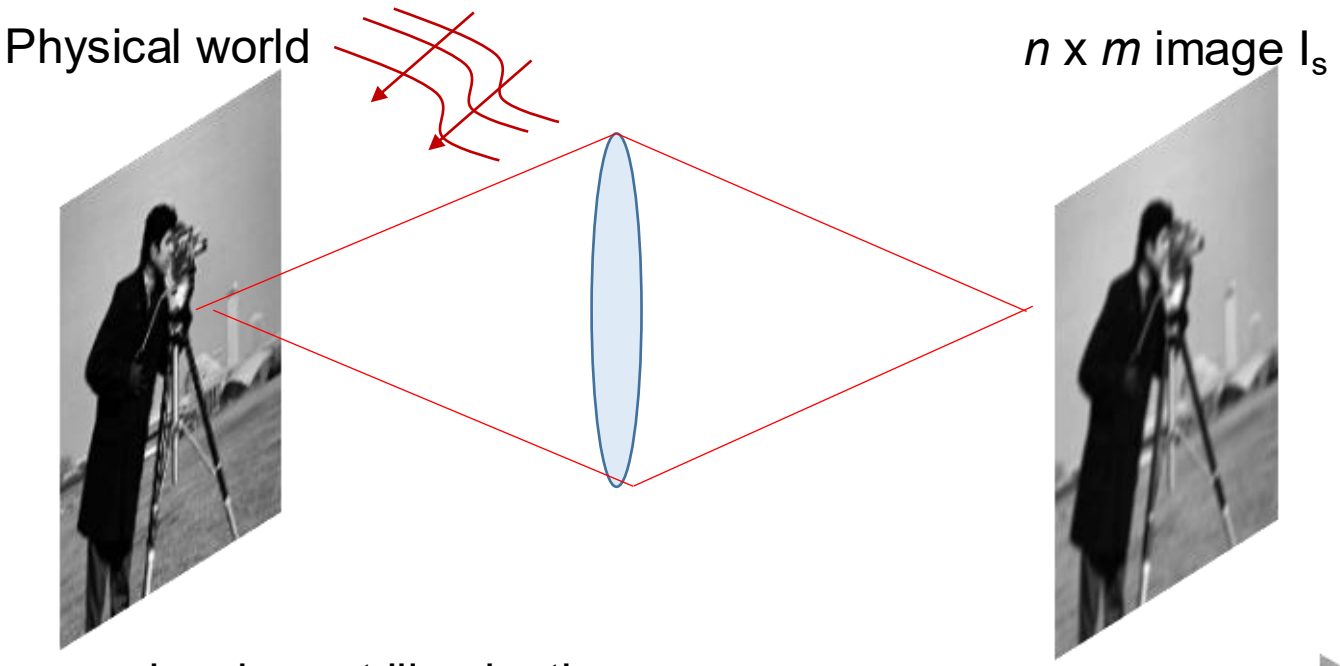
- Interpretation #3: Particle
- Model: Photons

Simple mathematical model of incoherent image formation

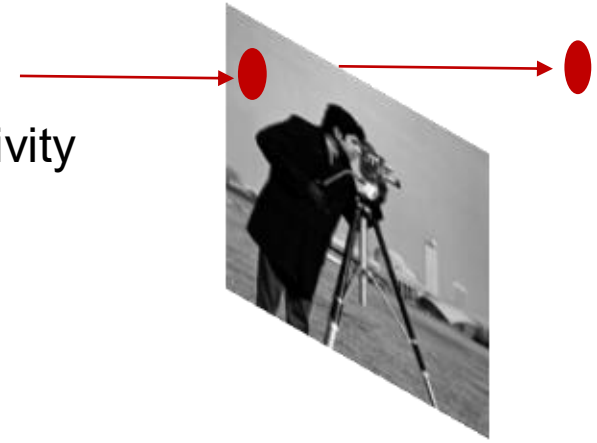


- Assume incoherent illumination
- Assume thin 2D object
- Object is real, non-negative map of absorption/reflectivity

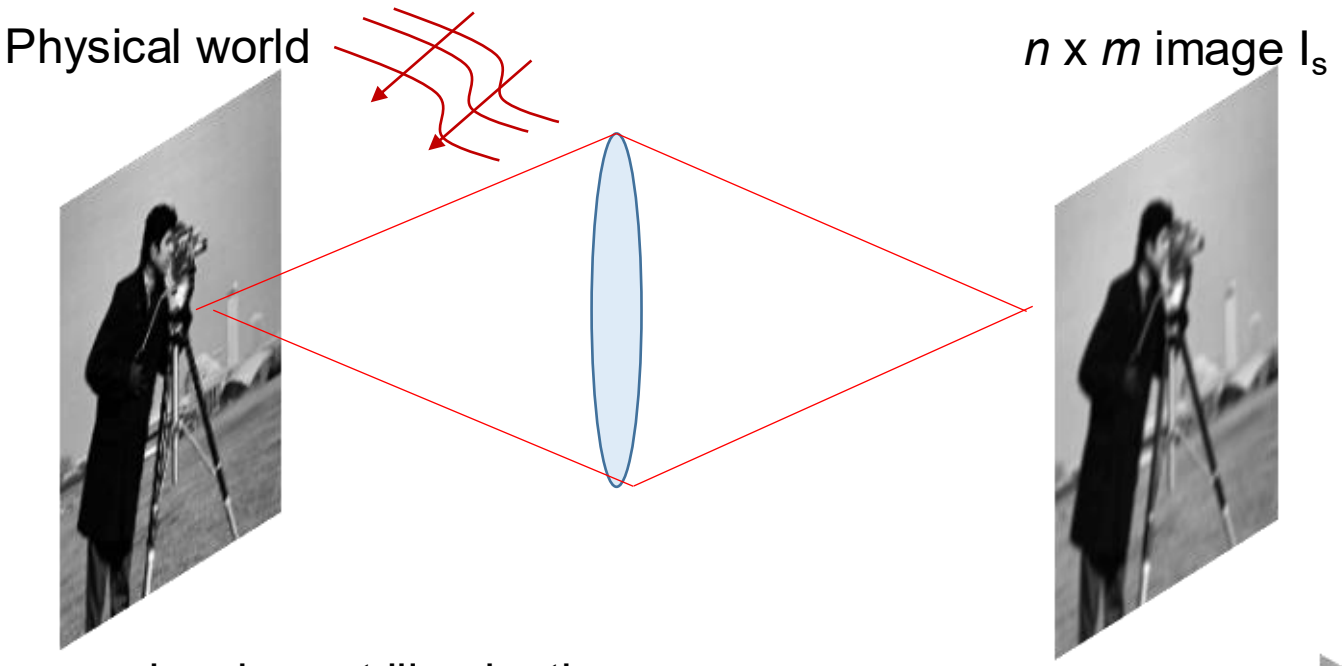
Simple mathematical model of incoherent image formation



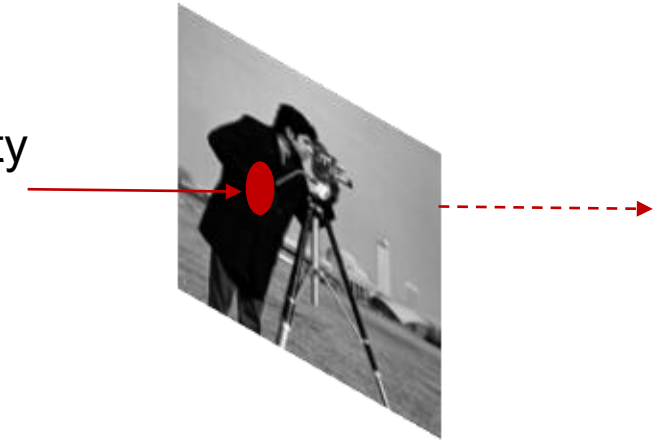
- Assume incoherent illumination
- Assume thin 2D object
- Object is real, non-negative map of absorption/reflectivity



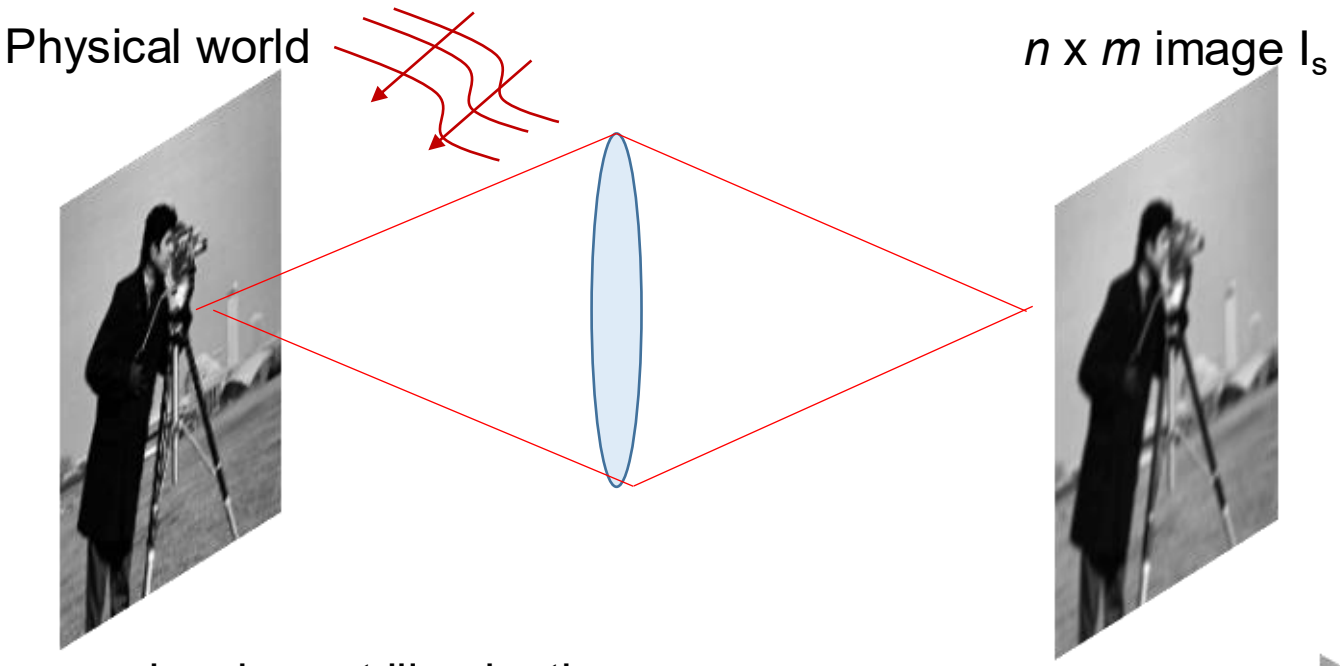
Simple mathematical model of incoherent image formation



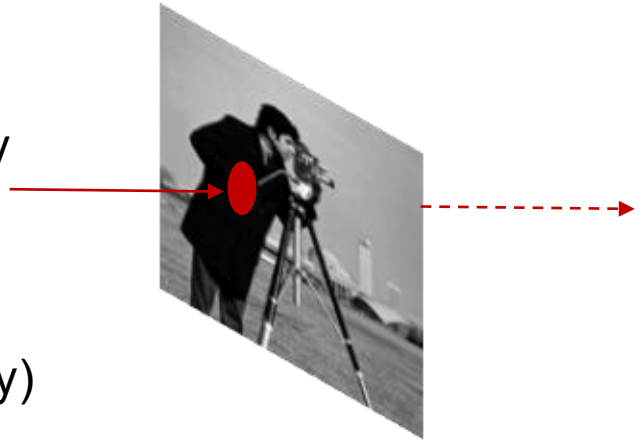
- Assume incoherent illumination
- Assume thin 2D object
- Object is real, non-negative map of absorption/reflectivity



Simple mathematical model of incoherent image formation

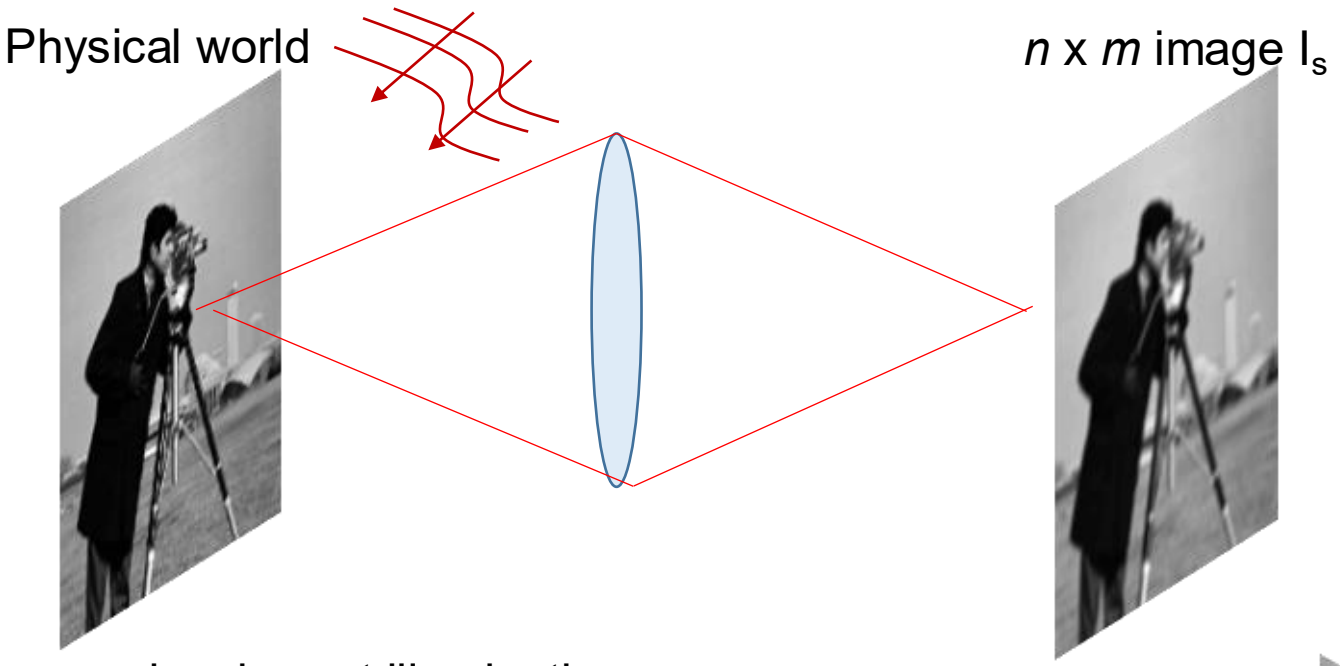


- Assume incoherent illumination
- Assume thin 2D object
- Object is real, non-negative map of absorption/reflectivity



Object transmission: $\mathbf{I_0}(x,y)$
Illumination pattern: $\mathbf{s}(x,y)$
Light exiting object surface: $\mathbf{I_e}(x,y) = \mathbf{I_0}(x,y) \circ \mathbf{s}(x,y)$

Simple mathematical model of incoherent image formation



- Assume incoherent illumination
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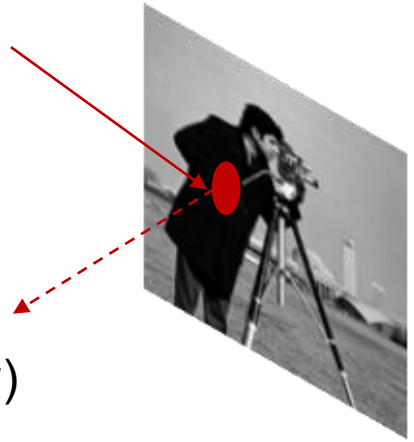
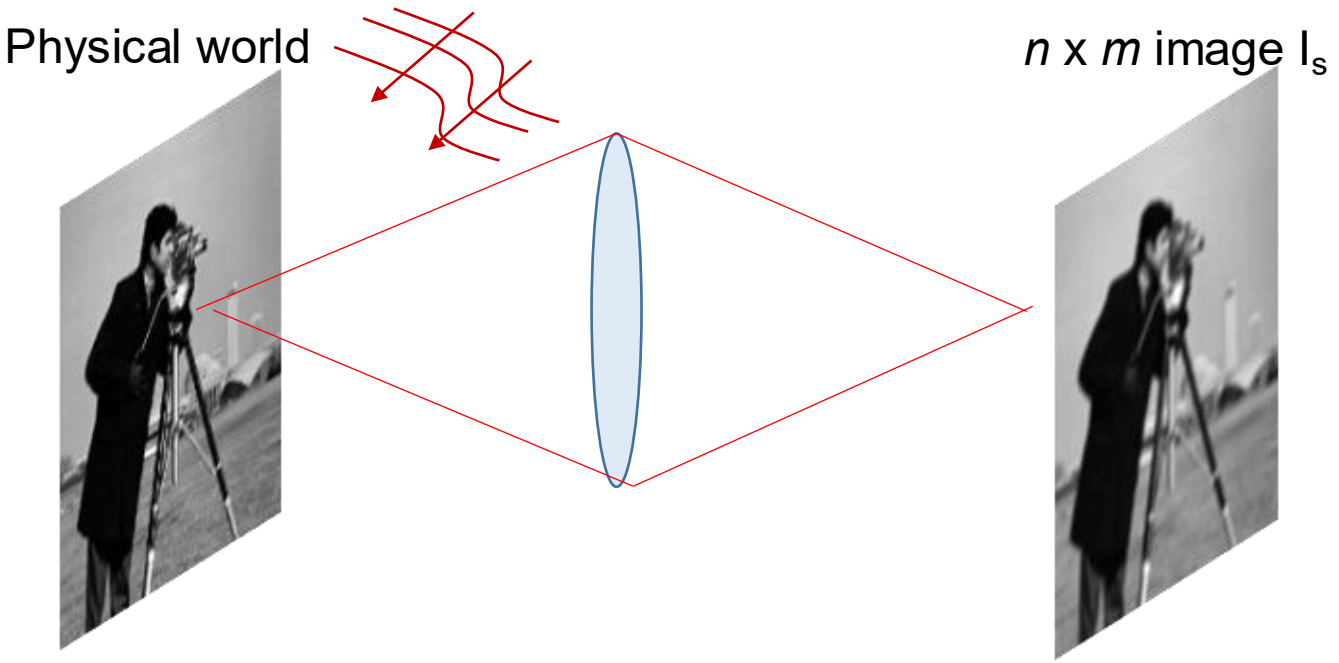


Object *reflectivity*: $\mathbf{I_0}(x,y)$
Illumination pattern: $\mathbf{s}(x,y)$
Light exiting object surface: $\mathbf{I_e}(x,y) = \mathbf{I_0}(x,y) \circ \mathbf{s}(x,y)$

Simple mathematical model of incoherent image formation



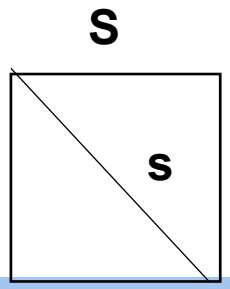
- Assume incoherent illumination
- Assume thin 2D object
- Object is real, non-negative map of absorption/reflectivity

Modeling incoherent illumination

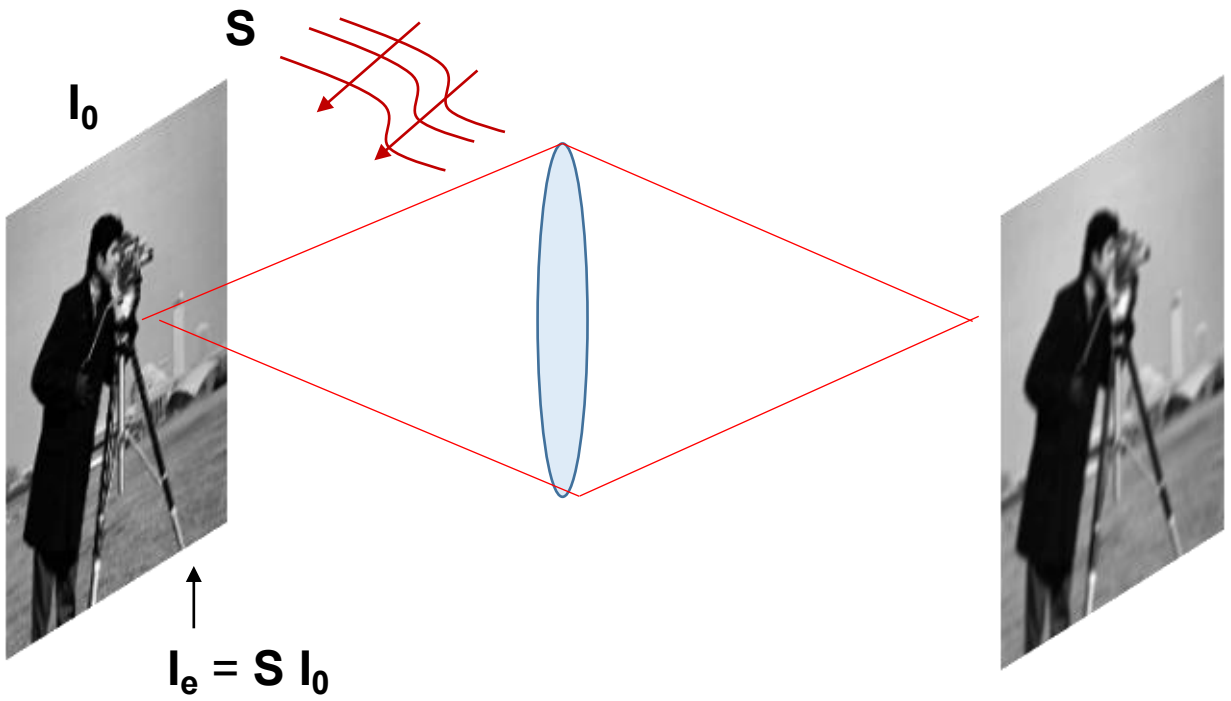
$$\mathbf{I_e}(x,y) = \mathbf{I_0}(x,y) \circ \mathbf{s}(x,y)$$

$$\mathbf{I_e} = \mathbf{S}\,\mathbf{I_0}$$

$\mathrm{diag}(\mathbf{S}) = \mathbf{s}$



Example #1: Optimized illumination pattern (one color)

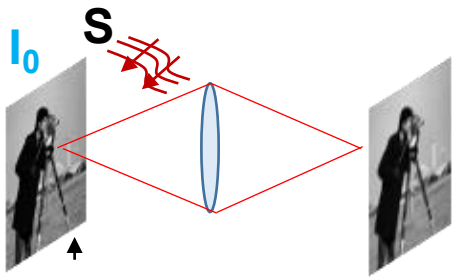


First, assume perfect camera:
intensity at image plane $I_p = I_e = S\ I_0$

Example #1: Optimized illumination pattern (one color)

Training data:
$[I_0(x, y), y]$
I_0:100 x 100
Label y: 1x2

Example #1: Optimized illumination pattern (one color)



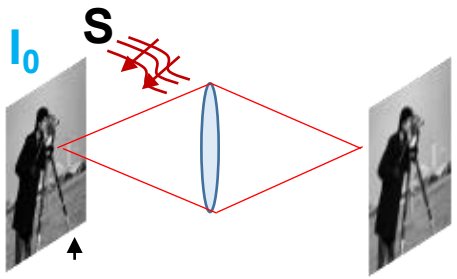
$[I_e(x, y), y]$

Training data:
$[I_0(x, y), y]$
I_0:100 x 100
Label y: 1x2

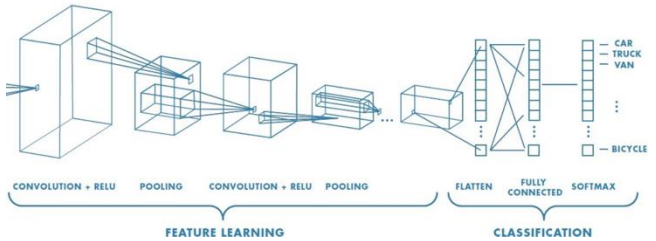
$I_e(x,y) = S\ I_0(x,y)$

Physical Layer

Example #1: Optimized illumination pattern (one color)



$[I_e(x, y), y]$



Training data:
$[I_0(x, y), y]$
I_0:100 x 100
Label y: 1x2

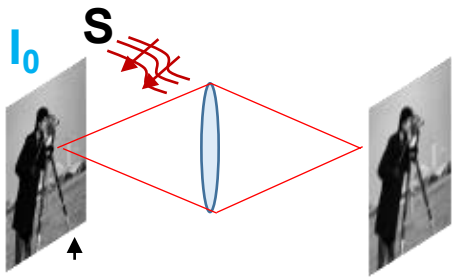
$I_e(x,y) = \mathbf{S}\ I_0(x,y)$

Physical Layer

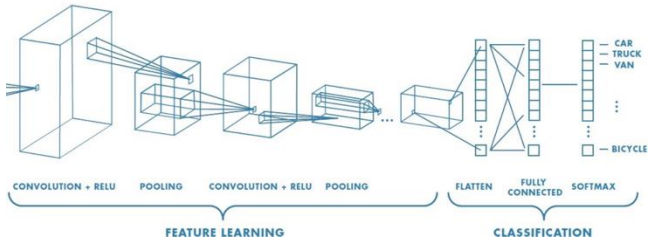
Task = $\mathbf{W_n} \ldots \mathrm{ReLU}[\mathbf{W_1}\ \mathrm{ReLU}[\mathbf{W_0}\ I_e] \ldots]$

Example #1: Optimized illumination pattern (one color)

deep imaging



$[I_e(x, y), y]$



Training data:
$[I_0(x, y), y]$
I_0:100 x 100
Label y: 1x2

$I_e(x,y) = \mathbf{S}\ I_0(x,y)$

Physical Layer

Task = $\mathbf{W_n} \ldots \mathrm{ReLU}[\mathbf{W_1}\ \mathrm{ReLU}[\mathbf{W_0}\ I_e] \ldots]$

Old Code

```
training_images = tf.placeholder(tf.float32, [image_size, None])
training_labels = tf.placeholder(tf.float32, [None, 3])
illumination_pattern = tf.truncated_normal([image_size, 1], stddev = 0.1)
illumination_matrix = tf.linalg.diag(illumination_pattern)
illumianted_images = tf.matmul(illumination_matrix, training_images)

#Now, train CNN of your choice using [illumianted_images, training_labels]
#Output of train/test will be CNN weights, classification performance AND illumination_pattern!
```

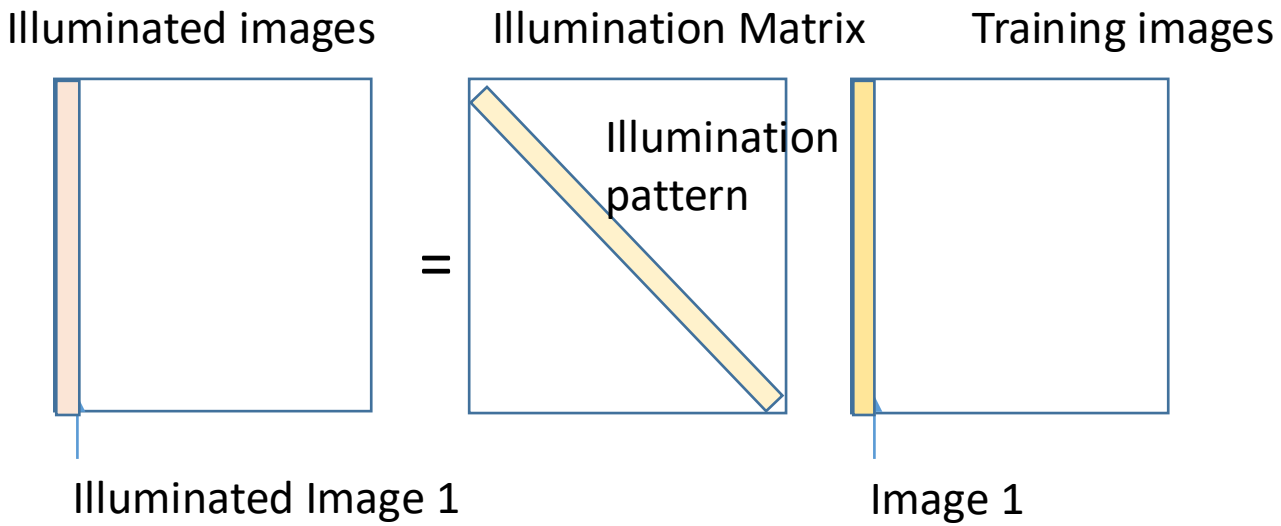
(Will show CoLab Notebook for implementation in Tensorflow 2.0)

Option 1: tf.linalg.matmul

Old Code

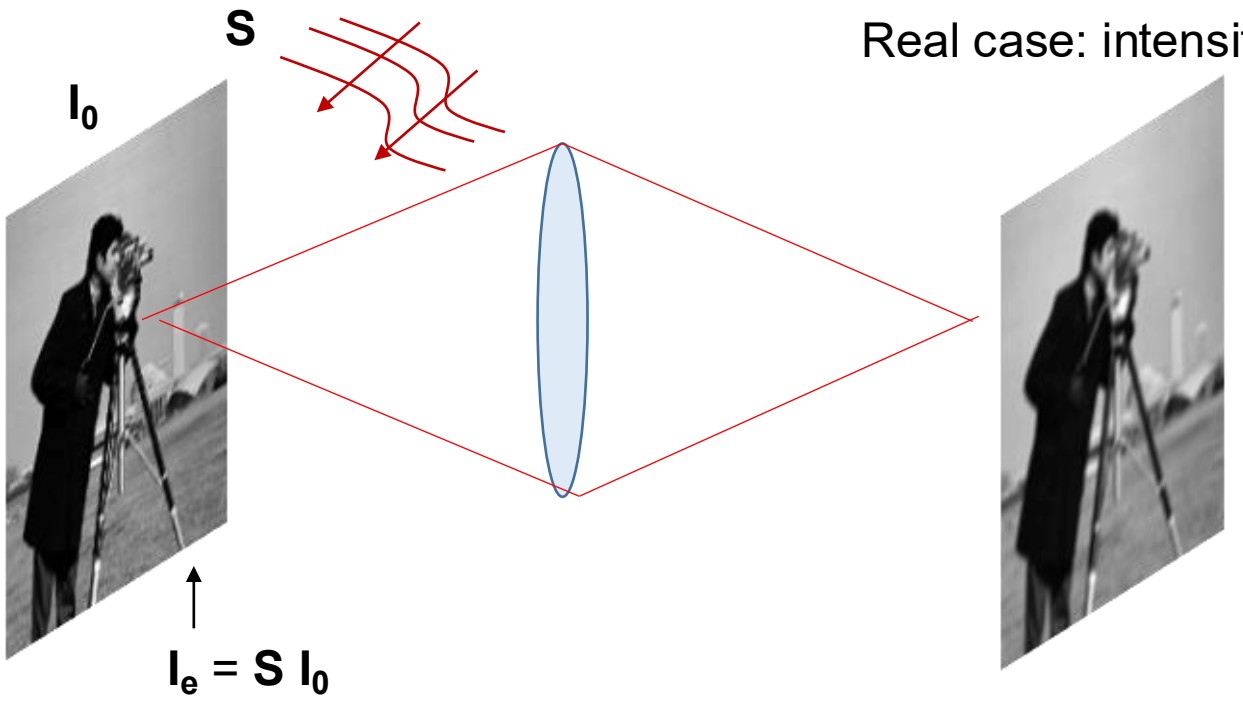
```
training_images = tf.placeholder(tf.float32, [image_size, None])
training_labels = tf.placeholder(tf.float32, [None, 3])
illumination_pattern = tf.truncated_normal([image_size, 1], stddev = 0.1)
illumination_matrix = tf.linalg.diag(illumination_pattern)
illumianted_images = tf.matmul(illumination_matrix, training_images)

#Now, train CNN of your choice using [illumianted_images, training_labels]
#Output of train/test will be CNN weights, classification performance AND illumination_pattern!
```



Option 2: tf.linalg.multiply (will show in CoLab Notebook)

Simple mathematical model of image formation



Real case: intensity at image plane I_p = **blurred**

Simple mathematical model of image formation

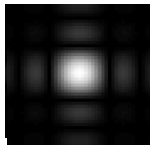
deep imaging

Lenses blur and rescale images:
(We'll learn how exactly next few weeks)

Input intensity

Convolution filter h

$*$



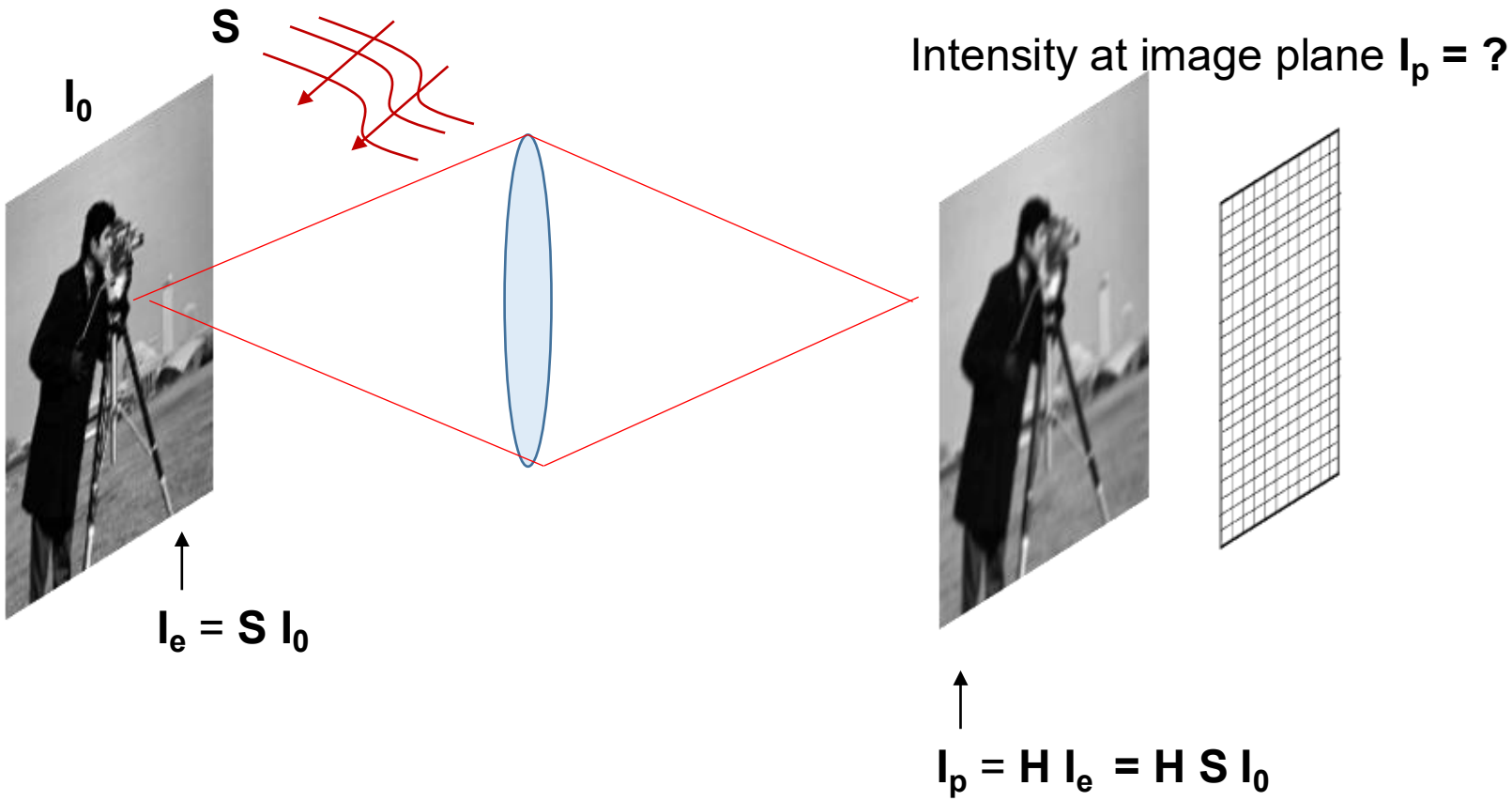
$=$

Output intensity

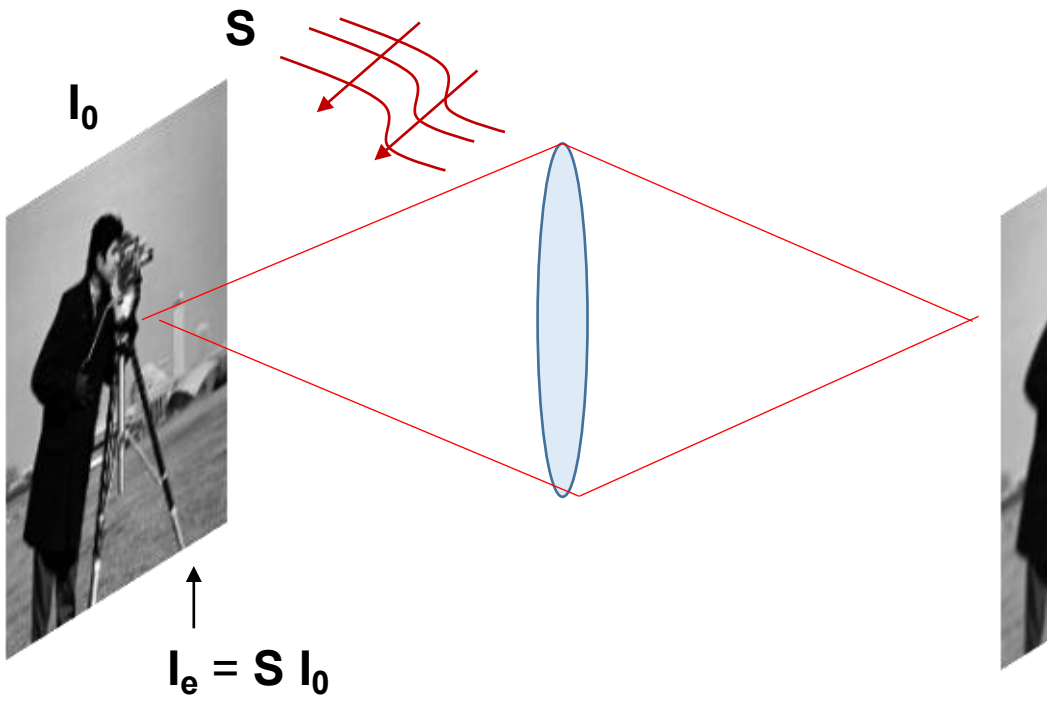
$\mathbf{I_e}(x/M, y/M) \quad * \quad \mathbf{h}(x,y) \quad = \quad \mathbf{I_p}(x,y)$

Assuming we've resized by M, $\mathbf{I_p = I_e * h = H I_e}$

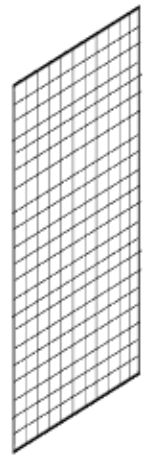
Simple mathematical model of image formation



Simple mathematical model of image formation



Discretization by detector ?



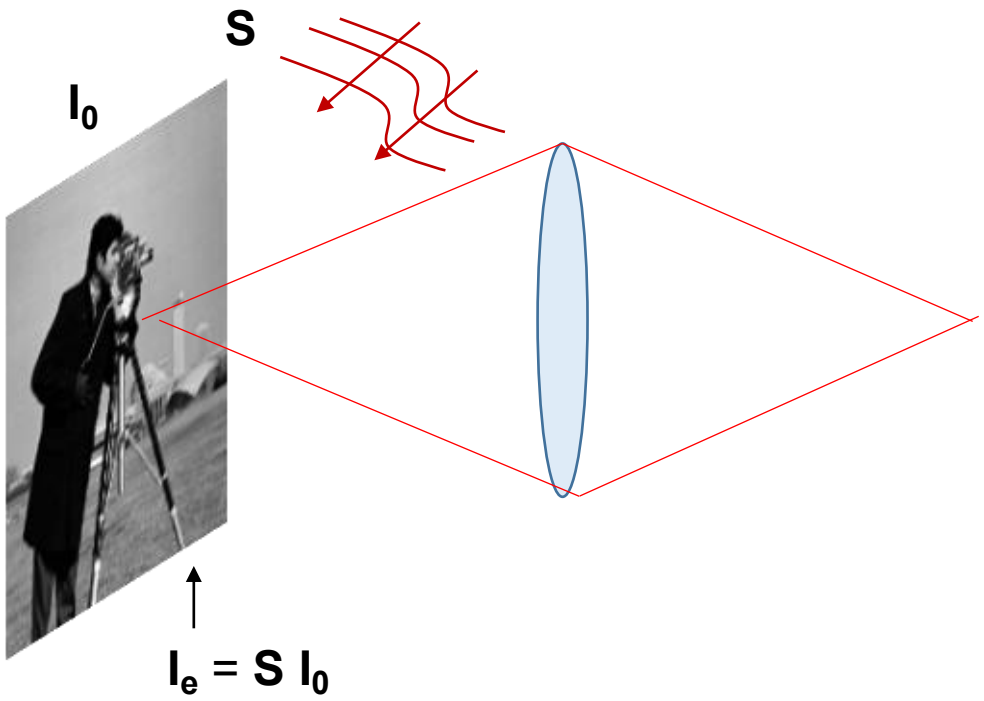
$I_p = H\ I_e = H\ S\ I_0$

Use downsampling matrix (sum-pooling)

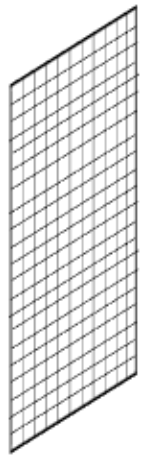
$D =$

$$\begin{bmatrix} 0.5\ 0.5\ 0\ 0\ 0\ \ldots. & & \\ & 0.5\ 0.5\ 0\ 0\ 0\ \ldots. & \\ & & 0.5\ 0.5\ 0\ 0\ 0\ \ldots. \\ \vdots & & \vdots \end{bmatrix}$$

Simple mathematical model of image formation



Discretization by detector ?

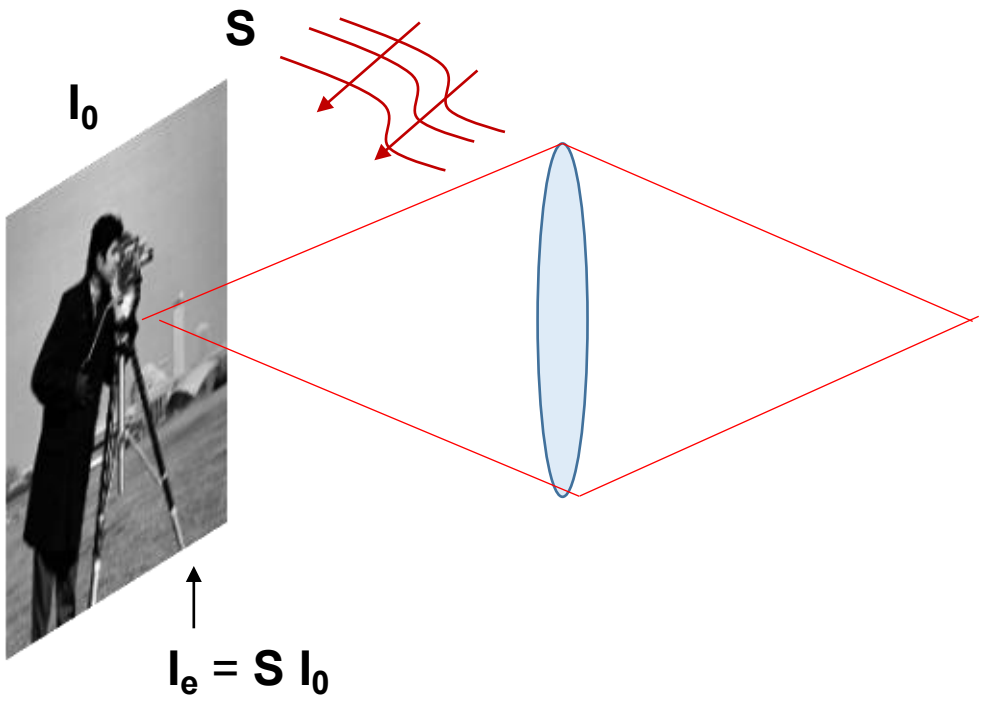


$$I_s = D\ I_p = D\ H\ S\ I_0$$

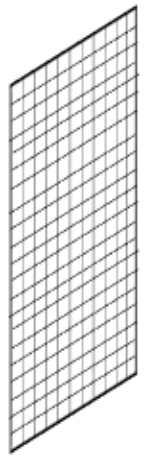
Use downsampling matrix (sum-pooling)

$$D = \begin{bmatrix} 0.5\ 0.5\ 0\ 0\ 0\ \ldots. & & \\ & 0.5\ 0.5\ \ 0\ 0\ 0\ \ldots. & \\ & & 0.5\ 0.5\ \ 0\ 0\ 0\ \ldots. \\ \vdots & & \vdots \end{bmatrix}$$

Simple mathematical model of image formation



Discretization by detector ?



$$I_s = D\ I_p = D\ H\ S\ I_0$$

$D =$

w1 w2 0 0 0 ....

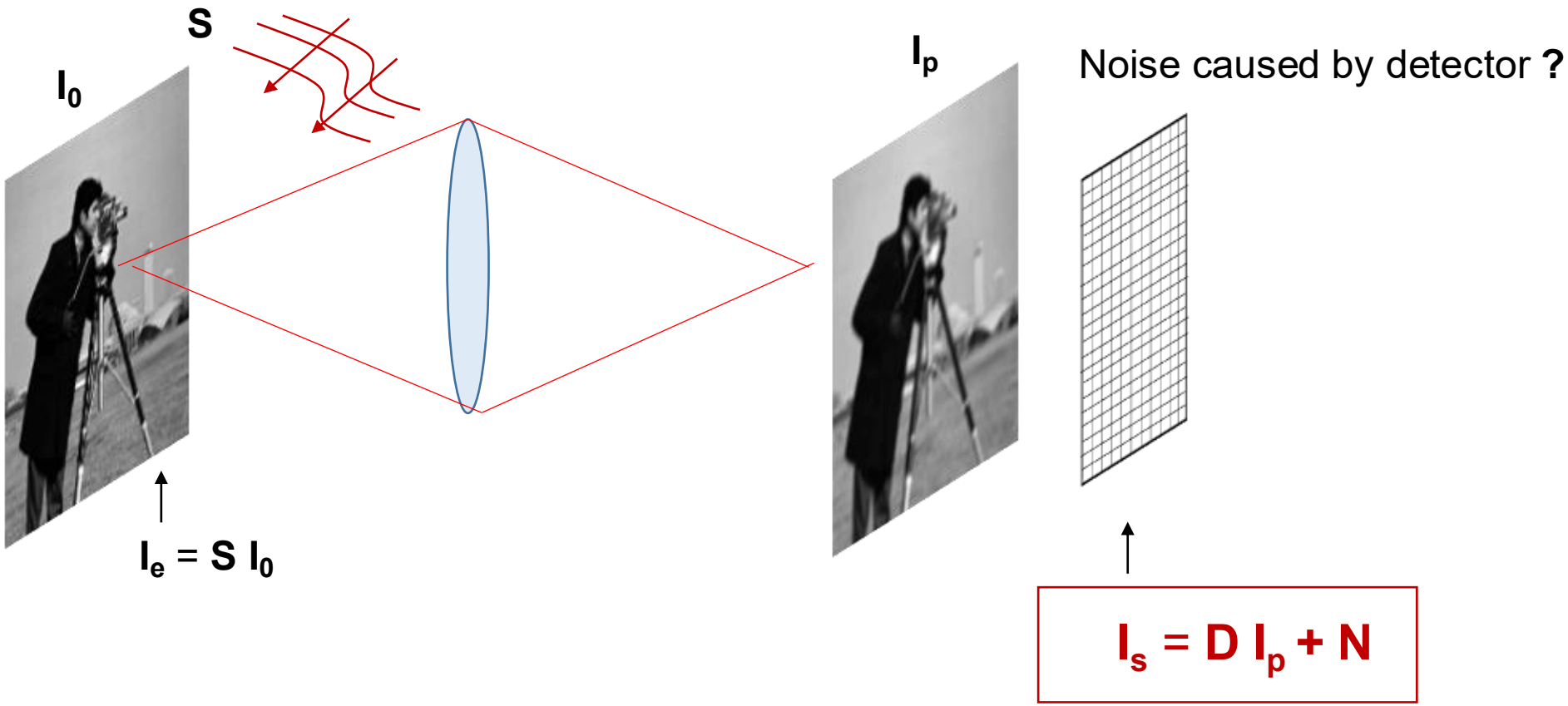
w3 w4 0 0 0 ....

w5 e6 0 0 0 ....

⋮ ⋮

*Can make these learnable weights

Simple mathematical model of image formation

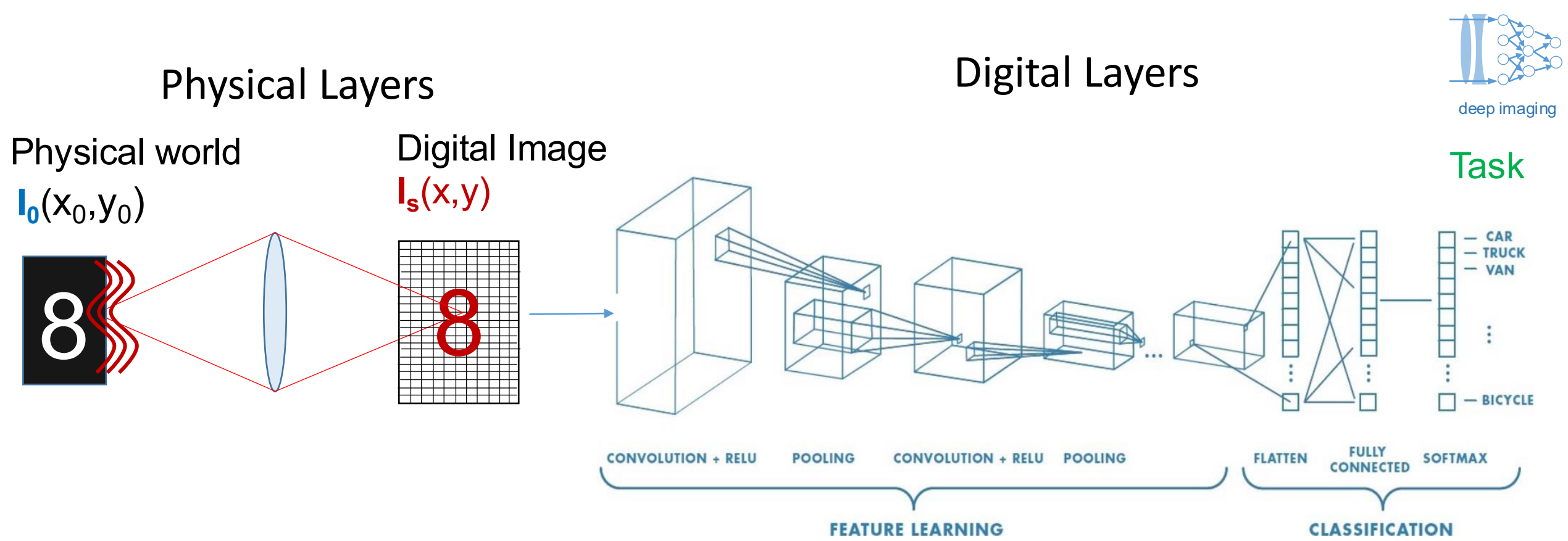


Can also add in detector-dependent noise N = k * np.random.randn(dx, dy)

(zero-mean Gaussian noise, for example)

Pause to take a look at:

physical_layers_example.ipynb



Digital layers

Physical layers

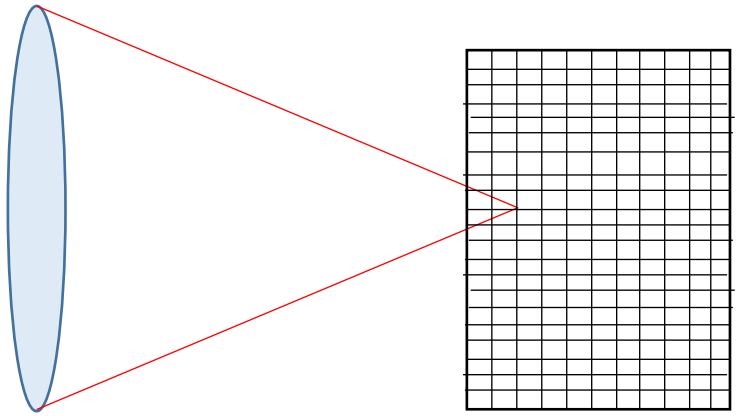
$$\text{Task} = \mathbf{W}_n \ldots \text{ReLU}[\mathbf{W}_1 \, \text{ReLU}[\mathbf{W}_0 \, f[\mathbf{I}_0]]\ldots]$$

$$\text{Task} = \mathbf{W}_n \ldots \text{ReLU}[\mathbf{W}_1 \, \text{ReLU}[\mathbf{W}_0 \, \mathbf{D} \, \mathbf{H} \, \mathbf{S} \, \mathbf{I}_0]\ldots]$$

Example #2: Optimized color filter for a grayscale camera

"Ground truth" object:
$I_0(x, y, \lambda)$
100 x 100 pix. x 30 spectral channels

Example #2: Optimized color filter for a grayscale camera



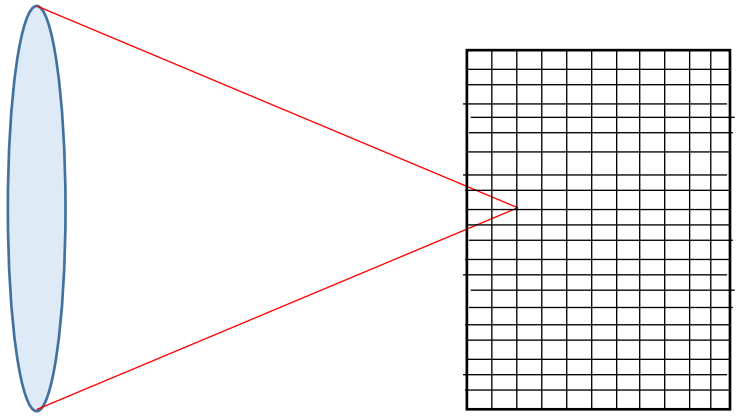
Monochromatic camera sensor

"Ground truth" object:

$I_0(x, y, \lambda)$

100 x 100 pix. x 30 spectral channels

Example #2: Optimized color filter for a grayscale camera

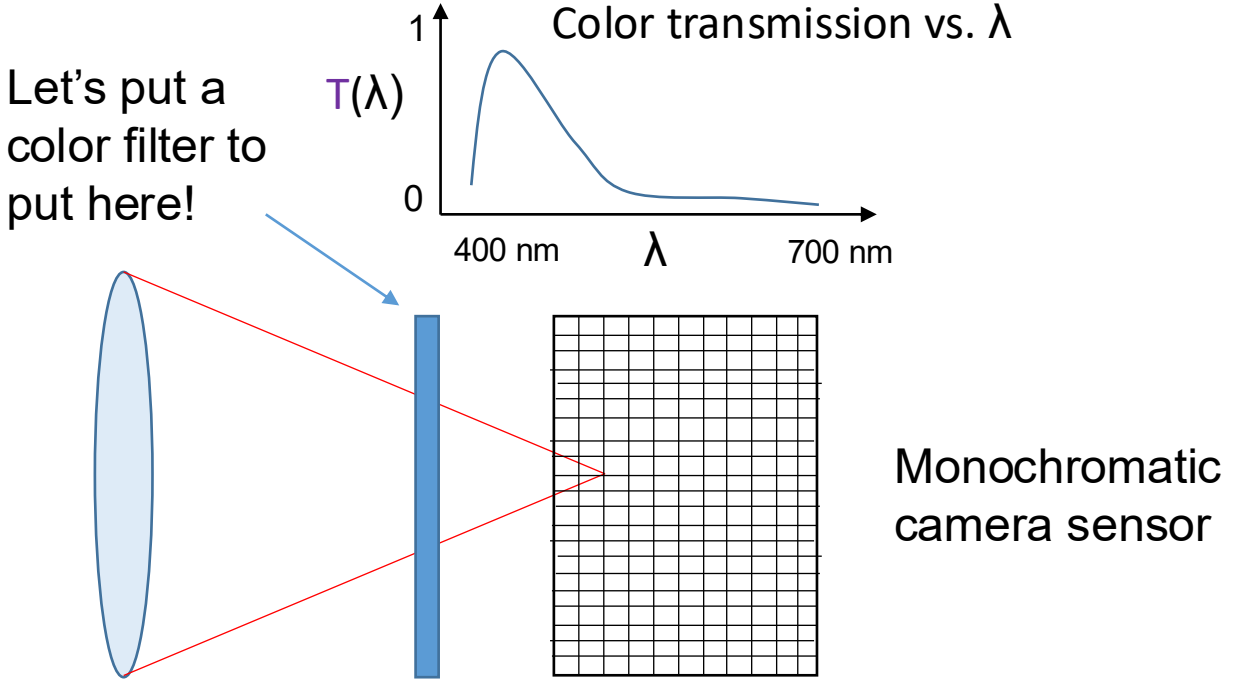


Monochromatic camera sensor

"Ground truth" object:
$I_0(x, y, \lambda)$
100 x 100 pix. x 30 spectral channels

$$I_s(x, y) = \sum_{\lambda} I_0(x, y, \lambda)$$

Example #2: Optimized color filter for a grayscale camera



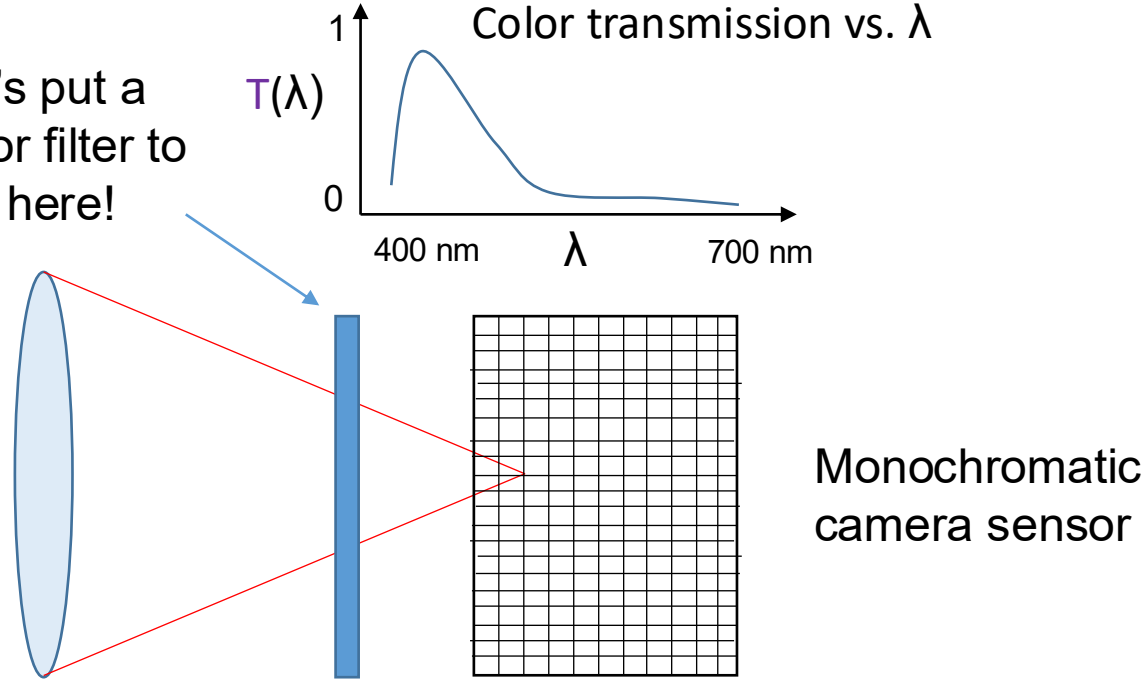
"Ground truth" object:

$I_0(x, y, \lambda)$

100 x 100 pix. x 30 spectral channels

Example #2: Optimized color filter for a grayscale camera

Let's put a color filter to put here!

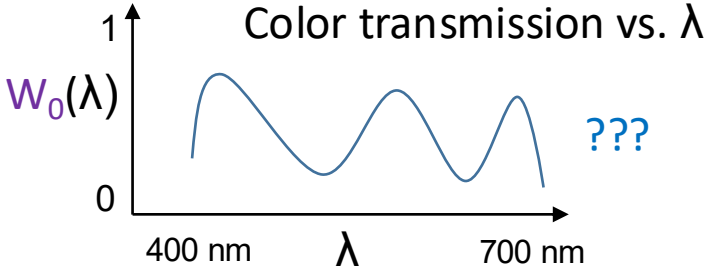


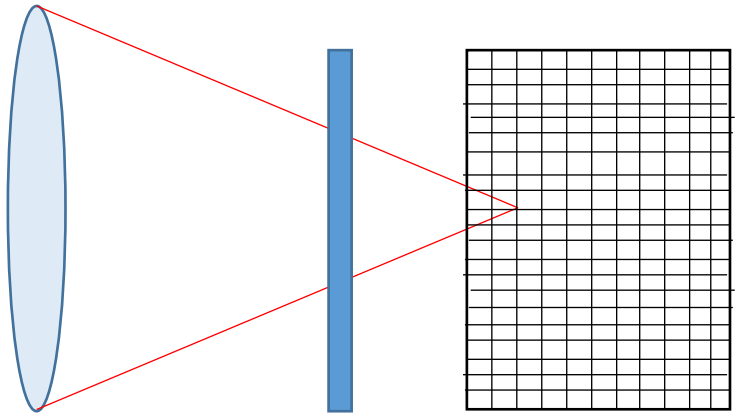
"Ground truth" object:
$I_0(x, y, \lambda)$
100 x 100 pix. x 30 spectral channels

$$I_s(x, y) = \sum_{\lambda} T(\lambda)\, I_0(x, y, \lambda)$$

Example #2: Optimized color filter for a grayscale camera

Design optimal color filter for classification:





Monochromatic camera sensor

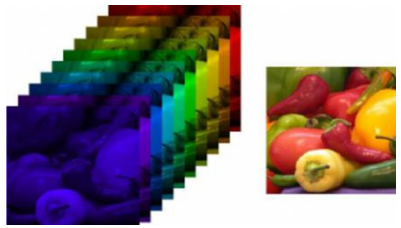
Training data:
$[I_0(x, y, \lambda), y]$
I_0:100 x 100 pix. x 30
Label y: 1x3 - pepper, broccoli, green beans

$$I_s(x, y) = \sum_{\lambda} W_0(\lambda)\, I_0(x, y, \lambda)$$

Physical Layer

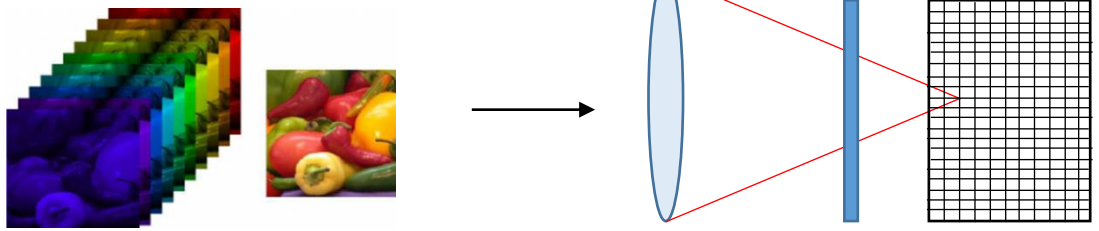
Example #2: Optimized color filter for a grayscale camera

deep imaging



Training data:
$[I_0(x, y, \lambda), y]$
I_0:100 x 100 x 30
Label y: 1x3

Example #2: Optimized color filter for a grayscale camera

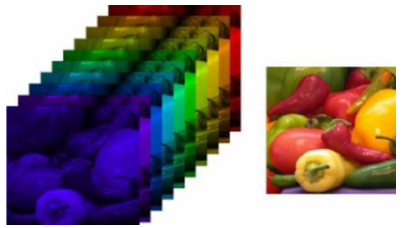


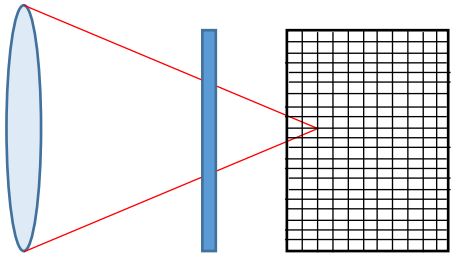
Training data:
$[I_0(x, y, \lambda), y]$
I_0:100 x 100 x 30
Label y: 1x3

$$I_s(x, y) = \sum_{\lambda} W_0(\lambda)\, I_0(x, y, \lambda)$$

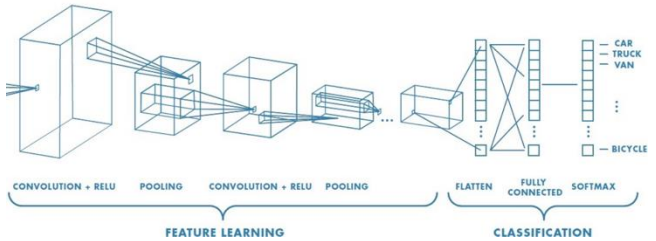
Physical Layer

Example #2: Optimized color filter for a grayscale camera





$[I_s(x, y), y]$



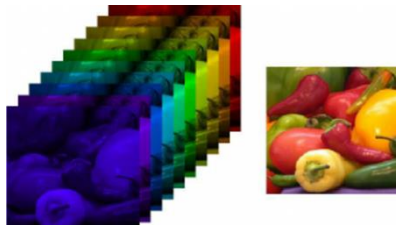
Training data:
$[I_0(x, y, \lambda), y]$
I_0:100 x 100 x 30
Label y: 1x3

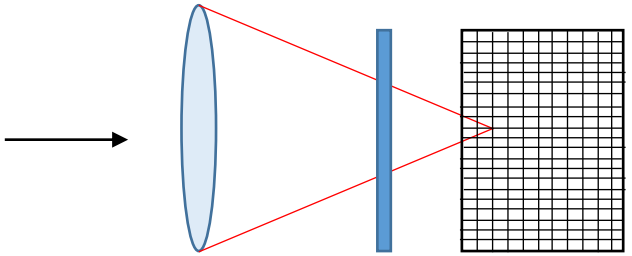
$$I_s(x, y) = \sum_{\lambda} W_0(\lambda)\, I_0(x, y, \lambda)$$

Physical Layer

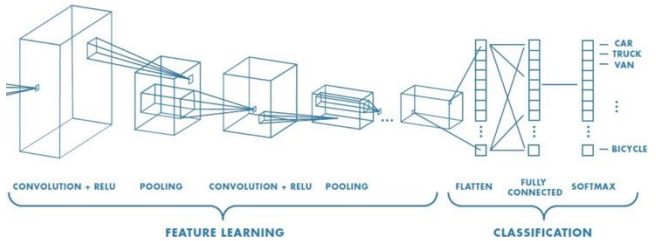
Task = $\mathbf{W_n} \ldots \mathrm{ReLU}[\mathbf{W_1}\, \mathrm{ReLU}[\mathbf{W_0}\, I_s] \ldots]$

Example #2: Optimized color filter for a grayscale camera





$[I_s(x, y), y]$



Training data:
$[I_0(x, y, \lambda), y]$
I_0:100 x 100 x 30
Label y: 1x3

$$I_s(x, y) = \sum_{\lambda} W_0(\lambda)\, I_0(x, y, \lambda)$$

Physical Layer

Task = $\mathbf{W_n} \ldots \mathrm{ReLU}[\mathbf{W_1}\, \mathrm{ReLU}[\mathbf{W_0}\, I_s] \ldots]$

```
multispectral_data = tf.placeholder(tf.float32, [None, num_colors, image_size])
veg_labels = tf.placeholder(tf.float32, [None, 3])
filter_weights = tf.truncated_normal([num_colors, 1], stddev = 0.1)
filtered_images = tf.einsum('aij,jk->aik', multispectral_data, filter_weights)

#Now, train CNN of your choice using [filtered_images, veg_labels]
#Output of training/testing will be CNN weights, classification performance AND filter_weights!
```

Example implementation with Tensorflow 1.0 code

Tensorflow: operations to sum along 3rd (or higher) dimension

deep imaging

Option 1: Einsum (shown as Tensorflow 1.0 code, and also applicable in Tensorflow 2.0)

```
filtered_images = tf.einsum('aij,jk->aik', multispectral_data, filter_weights)
```

Option 2: tf.reduce_sum

```
filtered_images = tf.reduce_sum(multispectral_data * filter_weights, axis=2)
```

Option 3: Locally connected conv2D with a 1x1 filter size

https://github.com/keras-team/keras/blob/master/keras/layers/local.py#L183

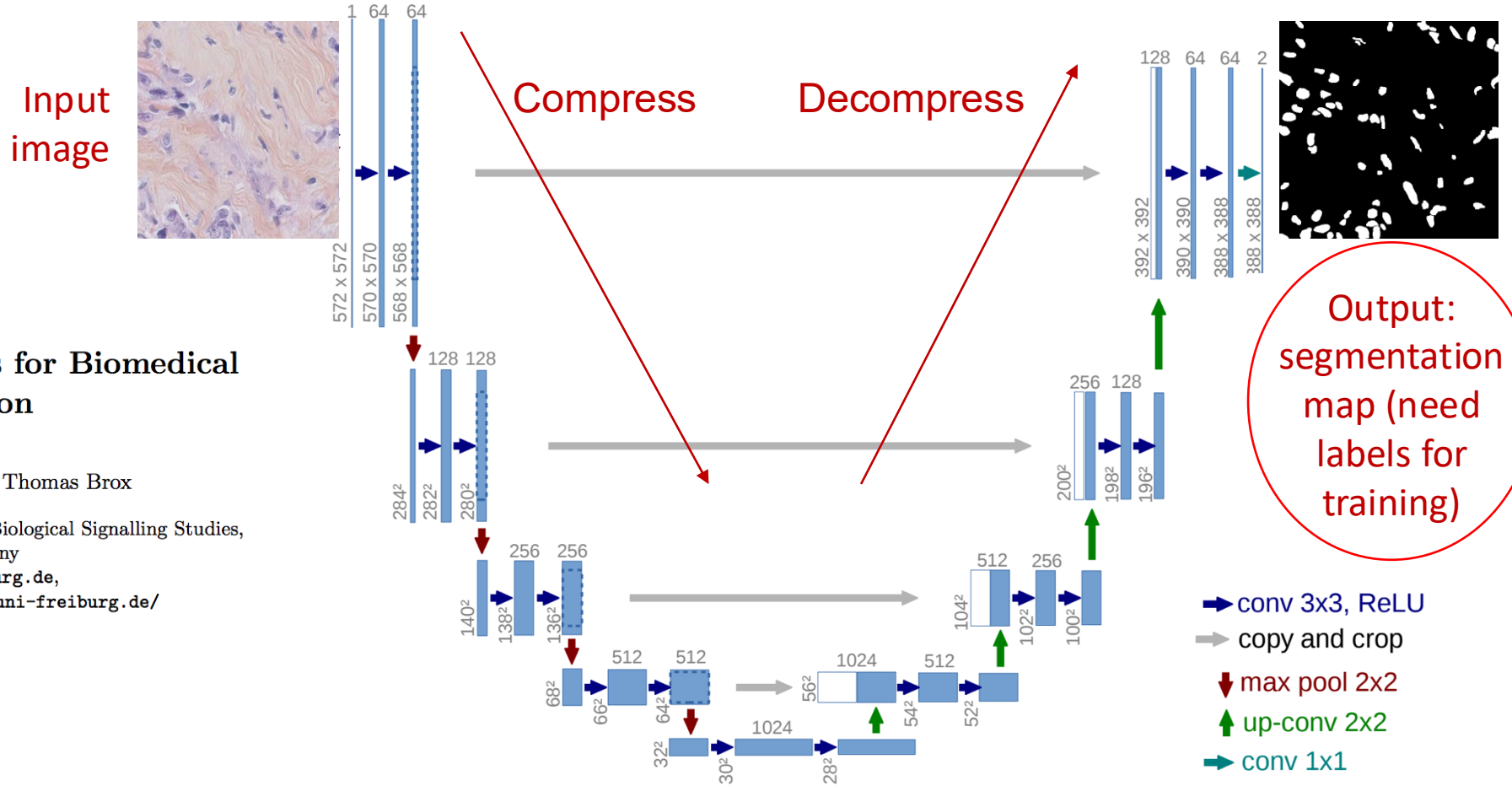
Pause to take a look at:

weighted_image_sum_example.ipynb

Example 3: learned illumination pattern for improved segmentation

deep imaging

U-Net Architecture

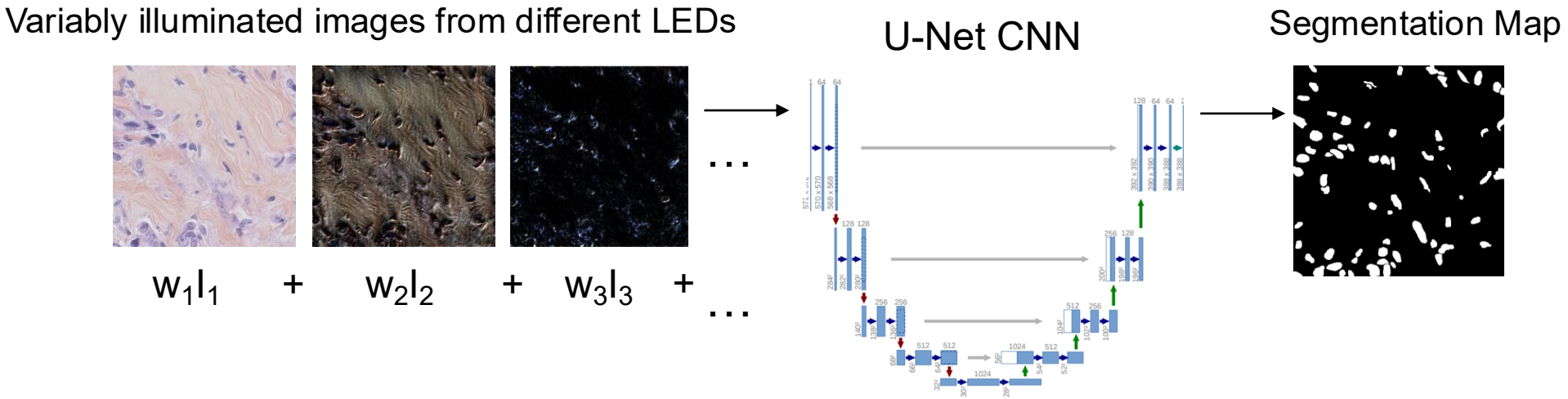


U-Net: Convolutional Networks for Biomedical Image Segmentation

Olaf Ronneberger, Philipp Fischer, and Thomas Brox

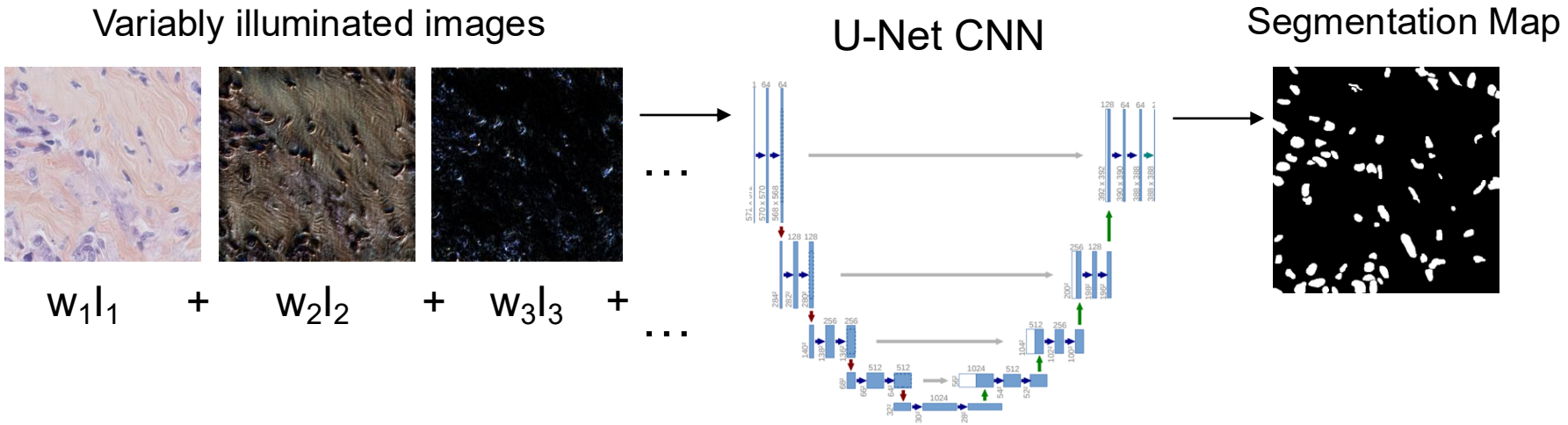
Computer Science Department and BIOSS Centre for Biological Signalling Studies,
University of Freiburg, Germany
ronneber@informatik.uni-freiburg.de,
WWW home page: http://lmb.informatik.uni-freiburg.de/

Example 3: learned illumination pattern for improved segmentation

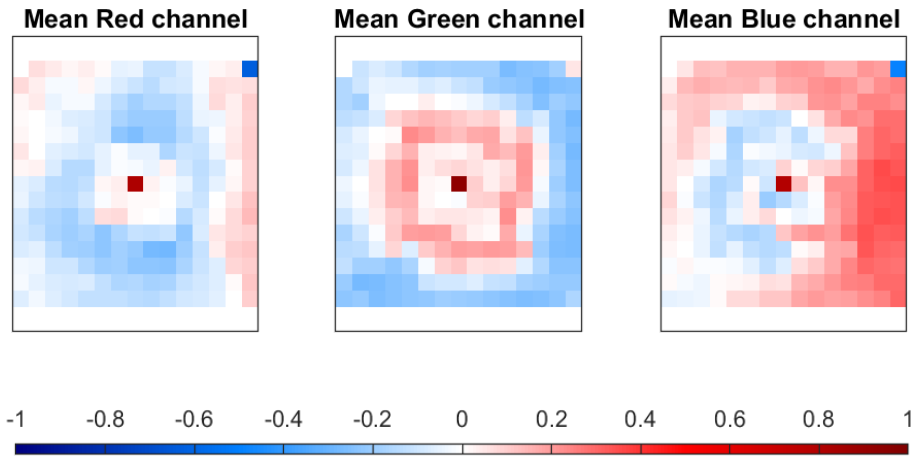


*If we allow w's here to be trainable weights, then we can find ideal brightnesses for different LEDs to illuminate a sample of interest!

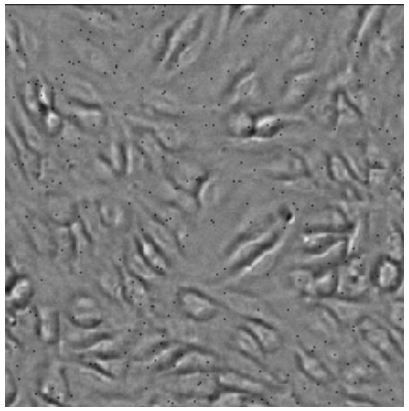
Example 3: learned illumination pattern for improved segmentation



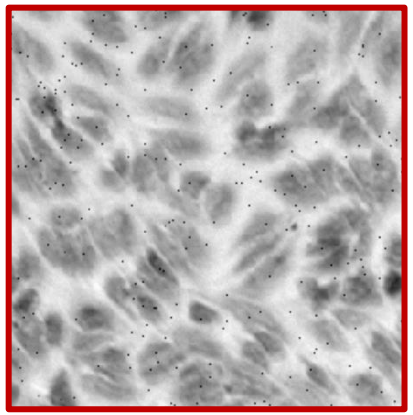
Optimized illumination for nuclei segmentation



Standard illumination



Learned illumination

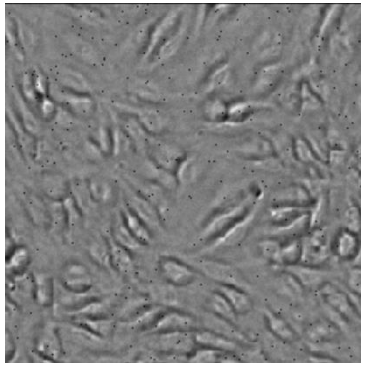


+5-10% accuracy

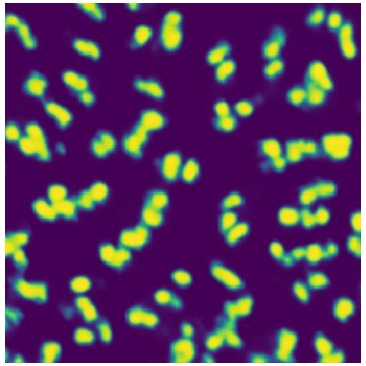
See C. Cooke et al., "Physics-enhanced machine learning for virtual fluorescence microscopy," ICCV (2021)

Image segmentation –current workflow

Capture: BF images



Capture: Fluorescence



(e.g., DAPI-stained nuclei)

Threshold

Segmentation Mask

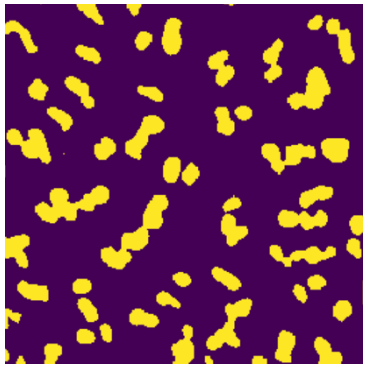
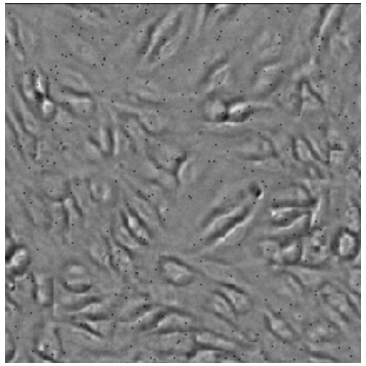


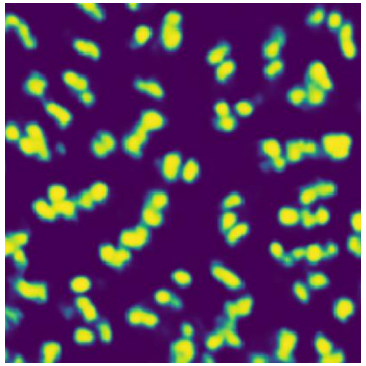
Image segmentation –current workflow

deep imaging

Capture: BF images



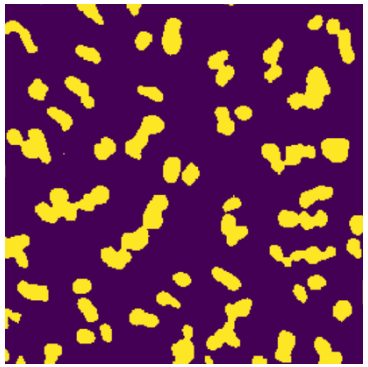
Capture: Fluorescence



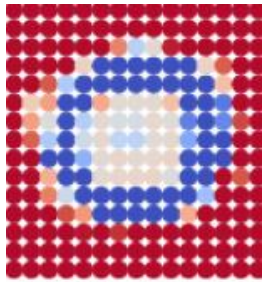
(e.g., DAPI-stained nuclei)

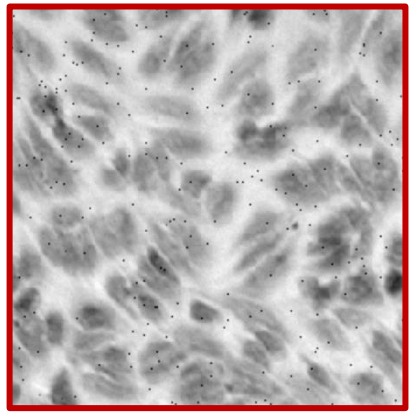
Threshold

Segmentation Mask



Learned illumination





Optimally illuminated

Inference via a trained U-Net

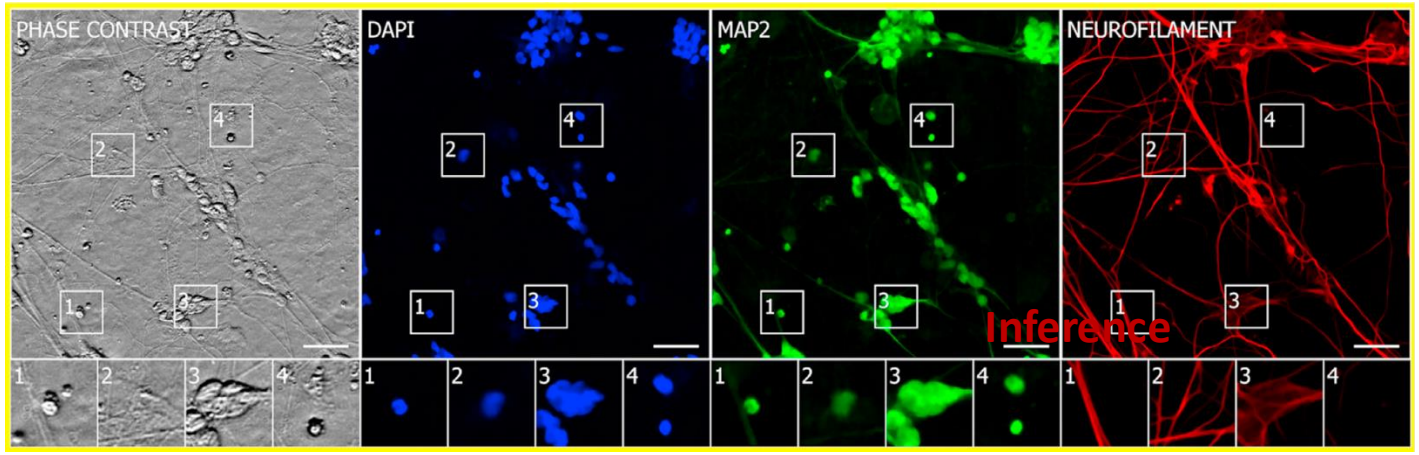
in silico labeling: fluorescence image inference from bright-field data

deep imaging

In Silico Labeling: Predicting Fluorescent Labels in Unlabeled Images

Eric M. Christiansen,[1,11,*] Samuel J. Yang,[1] D. Michael Ando,[1,9] Ashkan Javaherian,[2,9] Gaia Skibinski,[2,9] Scott Lipnick,[3,4,8,9] Elliot Mount,[2,10] Alison O'Neil,[3,10] Kevan Shah,[2,10] Alicia K. Lee,[2,10] Piyush Goyal,[2,10] William Fedus,[1,6,10] Ryan Poplin,[1,10] Andre Esteva,[1,7] Marc Berndl,[1] Lee L. Rubin,[3] Philip Nelson,[1,*] and Steven Finkbeiner[2,5,*]

[1]Google, Inc., Mountain View, CA 94043, USA
[2]Taube/Koret Center for Neurodegenerative Disease Research and DaedalusBio, Gladstone Institutes, San Francisco, CA 94158, USA
[3]Department of Stem Cell and Regenerative Biology, Harvard University, Cambridge, MA 02138, USA
[4]Department of Biomedical Informatics, Harvard Medical School, Boston, MA 02115, USA
[5]Departments of Neurology and Physiology, University of California, San Francisco, 94158, USA
[6]Montreal Institute of Learning Algorithms, University of Montreal, Montreal, QC, Canada
[7]Department of Electrical Engineering, Stanford University, Stanford, CA 94305, USA
[8]Center for Assessment Technology and Continuous Health, Massachusetts General Hospital, Boston, MA 02114, USA

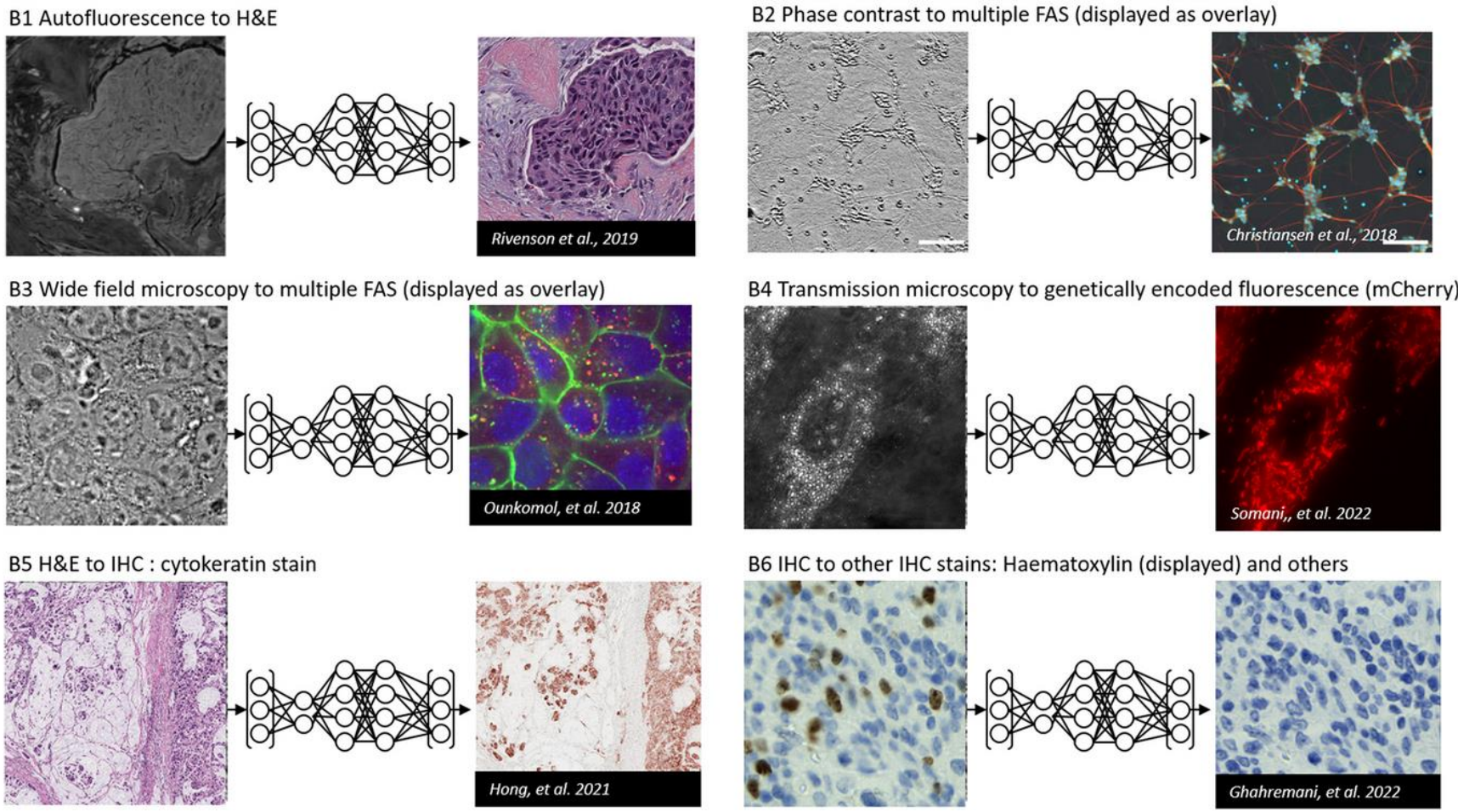


BF Focal stack (26+ images)

Task: bright-field to fluorescence image Inference

“Virtual Staining” – can be used to covert one image type to many others

deep imaging

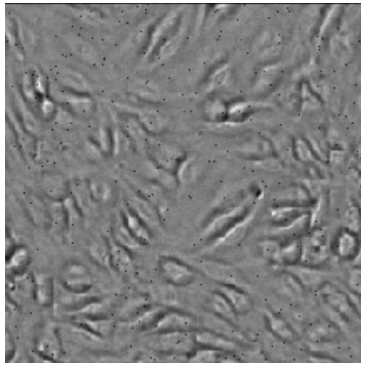


L. Kreiss et al., “Digital staining in optical microscopy using deep learning--a review,” Photonix (2024)
B. Bai et al., “Deep learning-enabled virtual histological staining of biological samples,” Nature Light Sci (2023)

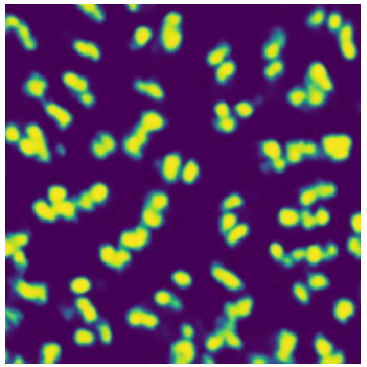
Image segmentation versus *in silico* labeling (fluorescence inference)

deep imaging

Capture: Bright field



Capture: Fluorescence



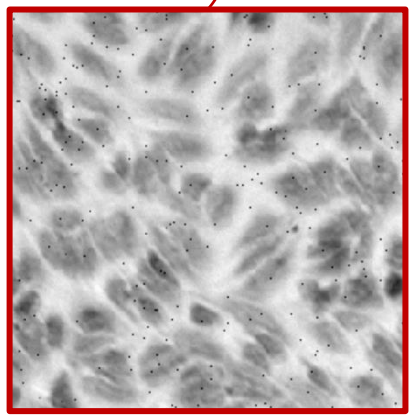
Threshold

Segmentation Mask

Directly infer the fluorescence image

Learned illumination for fluorescent image inference?

?



Optimally illuminated

Multiple Patterns for Fluorescence image inference

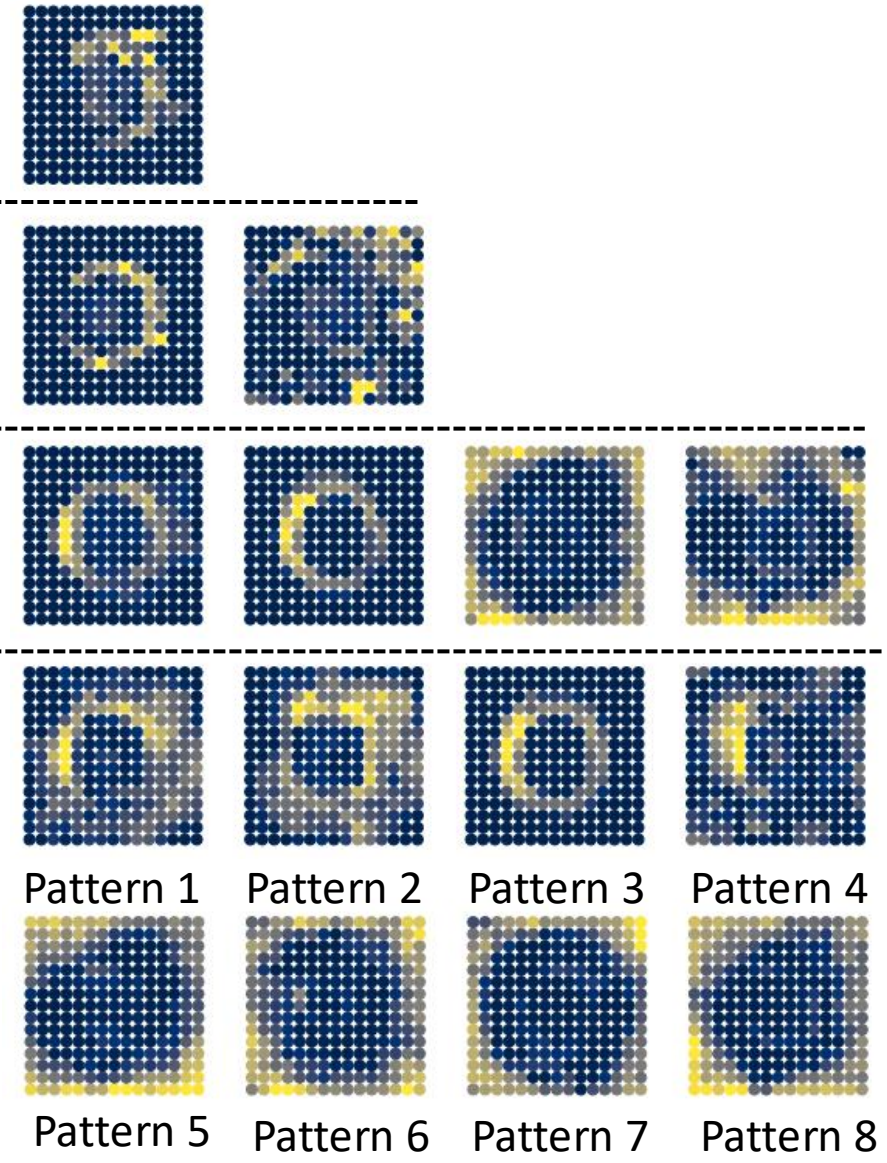
deep imaging

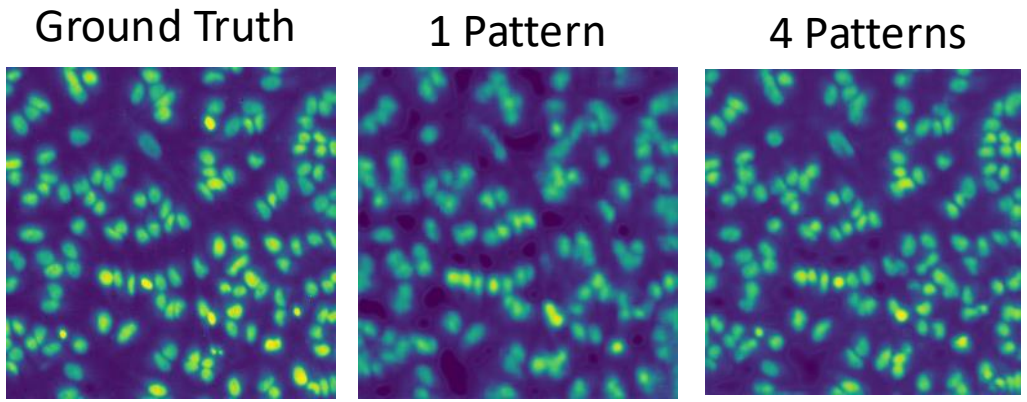
1x Pattern Optimization

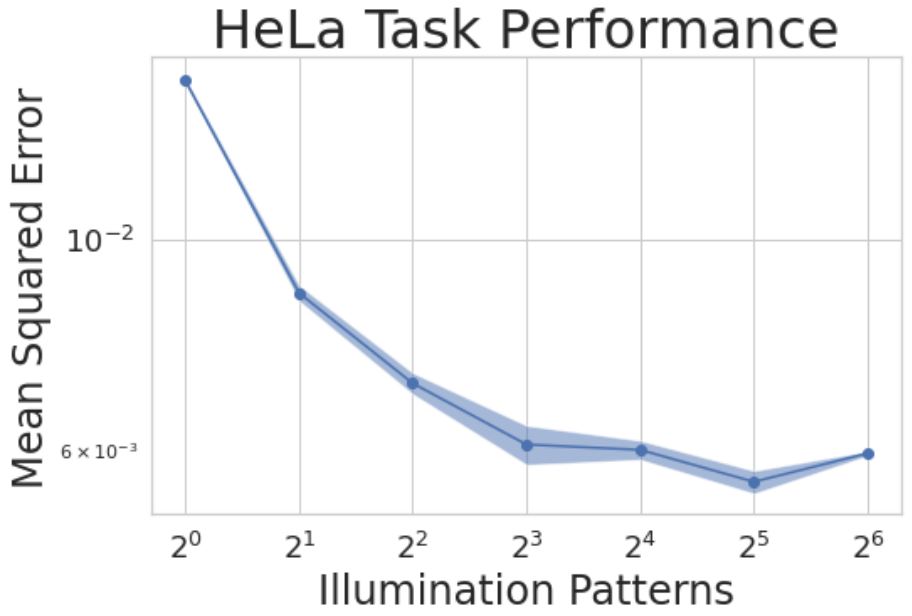
2x Pattern Optimization

4x Pattern Optimization

8x Pattern Optimization







See C. Cooke et al., "Physics-enhanced machine learning for virtual fluorescence microscopy," ICCV (2021)

Summary: simple physical layers for incoherent imaging

- Deal with sample/image intensities I, real and non-negative
- Effect of illumination is element-wise multiplication

$$I_e(x,y) = \mathbf{S}\, I_0(x,y)$$

λ

- Imaging systems blur the object via point-spread function matrix **H**

$$I_b(x,y) = \mathbf{H}\, I_0(x,y)$$

- Discrete pixels down-sample the object via

$$I_d(x,y) = \mathbf{D}\, I_0(x,y)$$

- Add noise into measurement

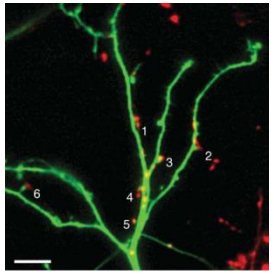
$$I_N(x,y) = \mathbf{D}\, I_0(x,y) + \mathbf{N}$$

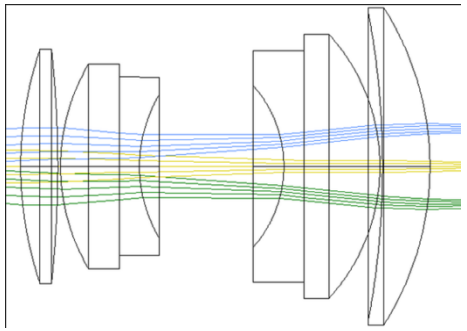
- Different colors add linearly

$$I_s(x, y) = \Sigma\, I_0(x, y, \lambda)$$

What is light and how can we model it?

- Interpretation #1: Radiation (*Incoherent*)
- Model: Rays

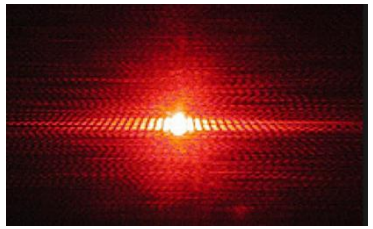


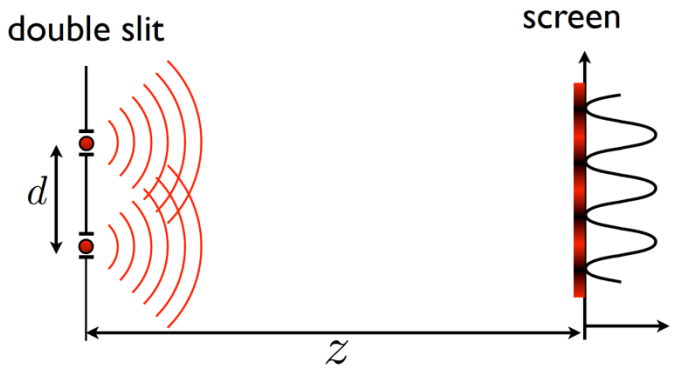


- Real, non-negative
- Models absorption and brightness

$$I_{tot} = I_1 + I_2$$

- Interpretation #2: Electromagnetic wave (*Coherent*)
- Model: Waves





- Complex field
- Models Interference

$$E_{tot} = E_1 + E_2$$

Alternative framework: Modeling coherent radiation as a wave